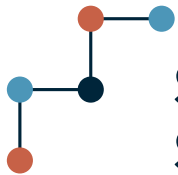


Frequency Dynamics of Power Grids

Julian Fritzscht

Young Researchers' Day

16. September 2022



**Swiss National
Science Foundation**

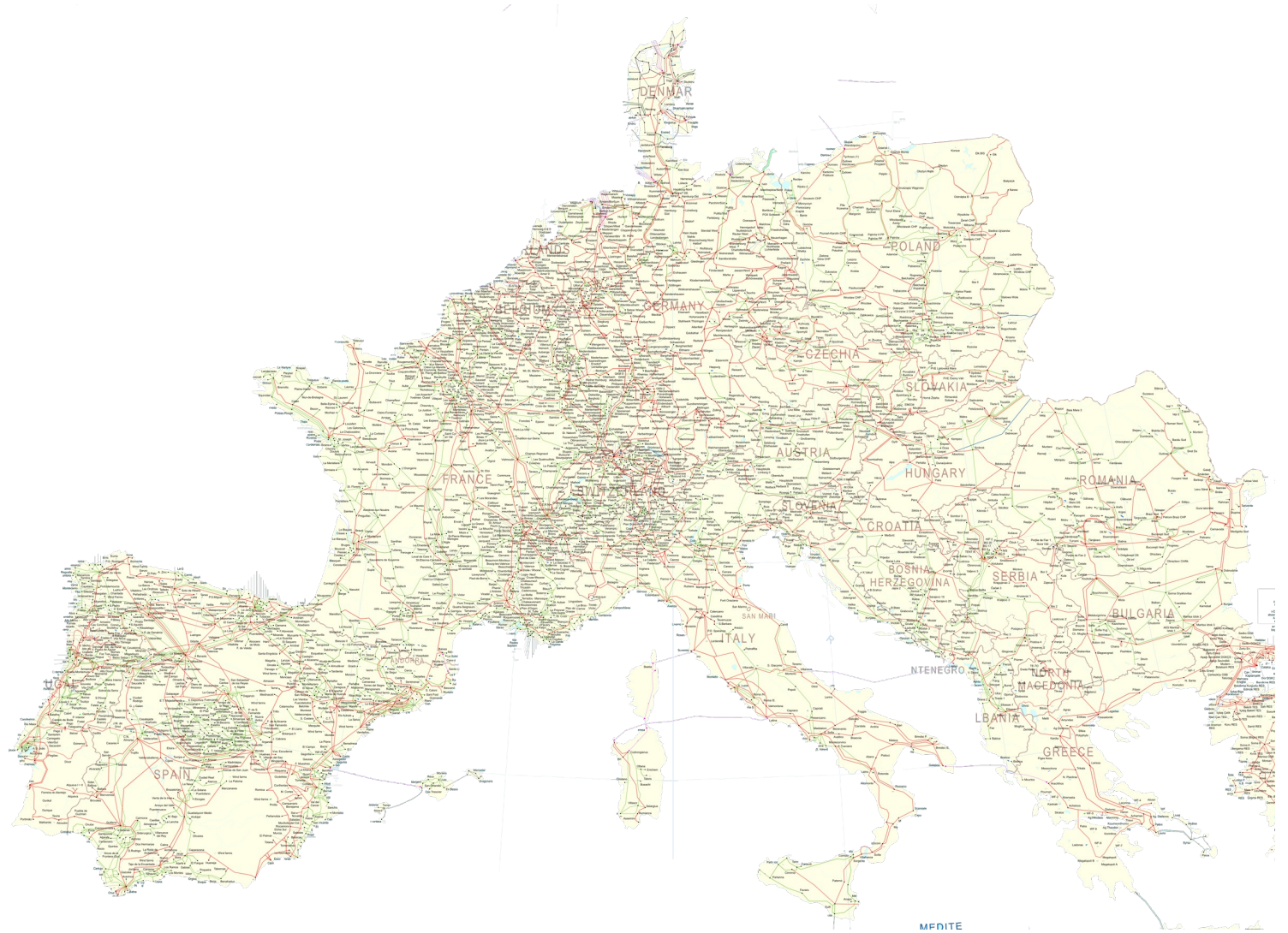


**UNIVERSITÉ
DE GENÈVE**

FACULTY OF SCIENCE
Department of Quantum
Matter Physics

Hes·SO  **VALAIS
WALLIS**
School of
Engineering 

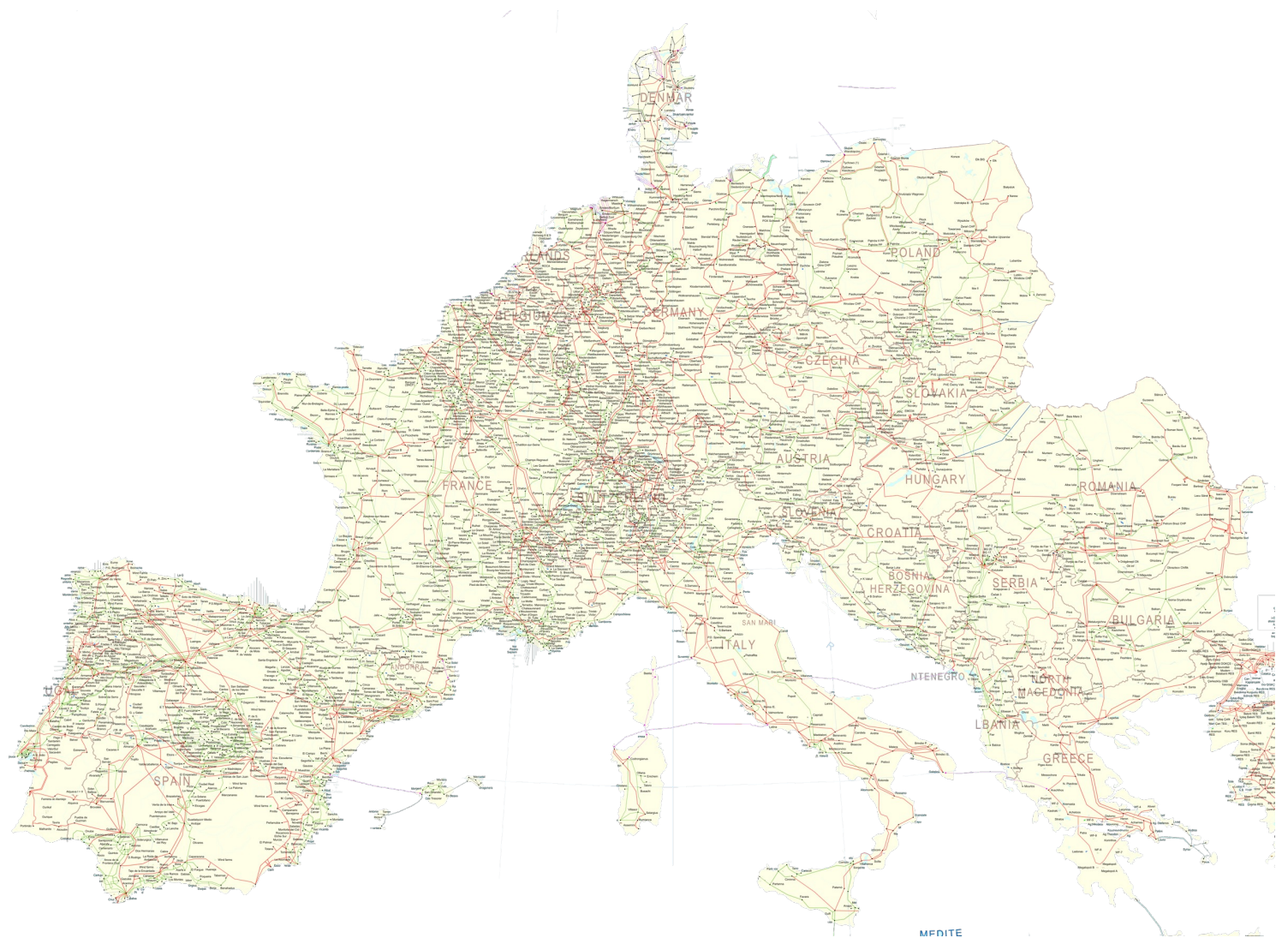
Motivation



<https://www.entsoe.eu/data/map/downloads/>

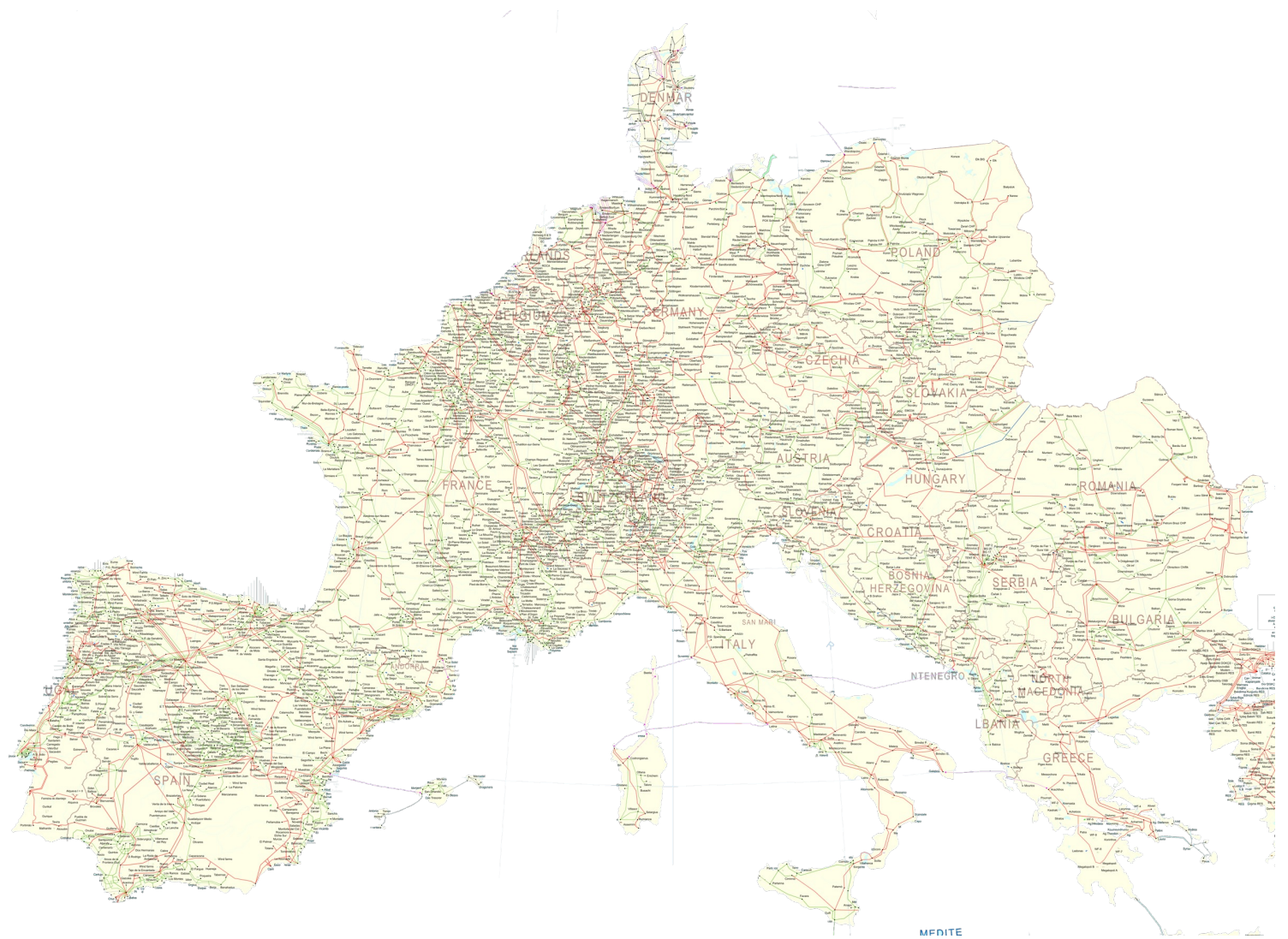
Motivation

- Power grids are large connected networks



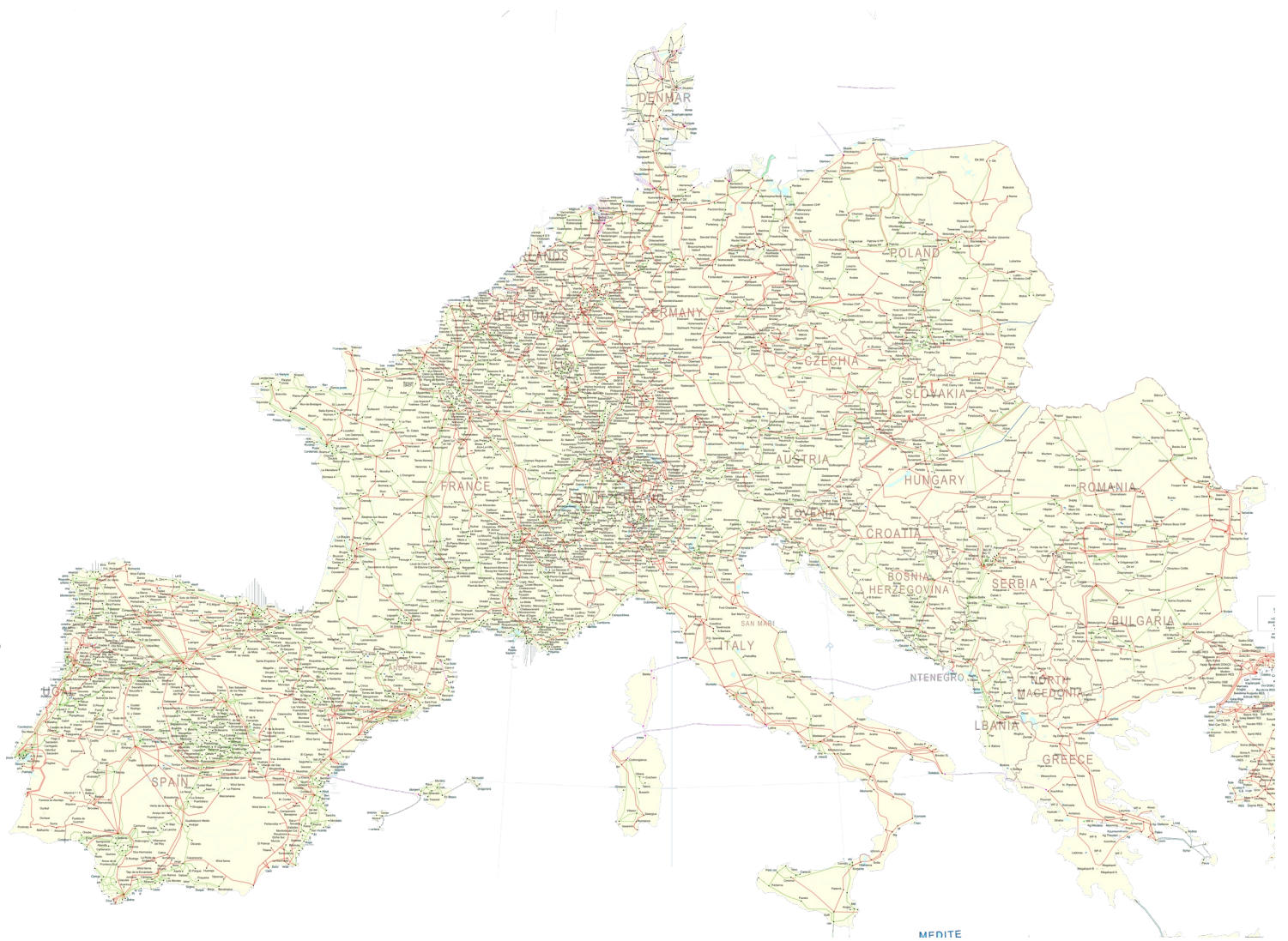
Motivation

- Power grids are large connected networks
- How do single components interact?

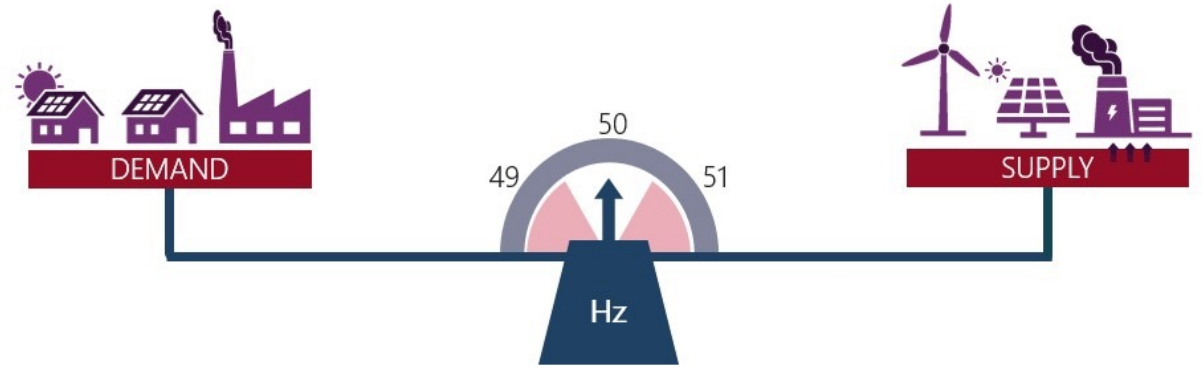


Motivation

- Power grids are large connected networks
- How do single components interact?
- Can we use techniques from theoretical physics?



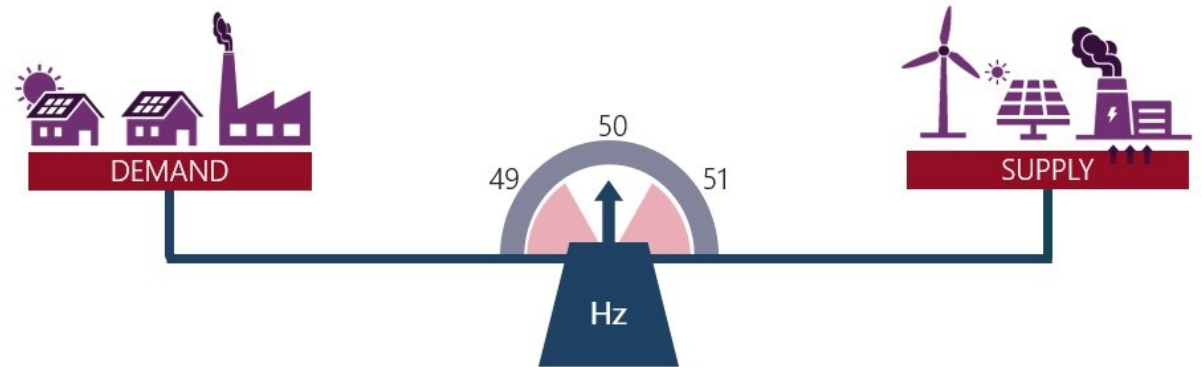
Grid Frequency



<https://aemo.com.au/learn/energy-explained/energy-101/energy-explained-frequency>

Grid Frequency

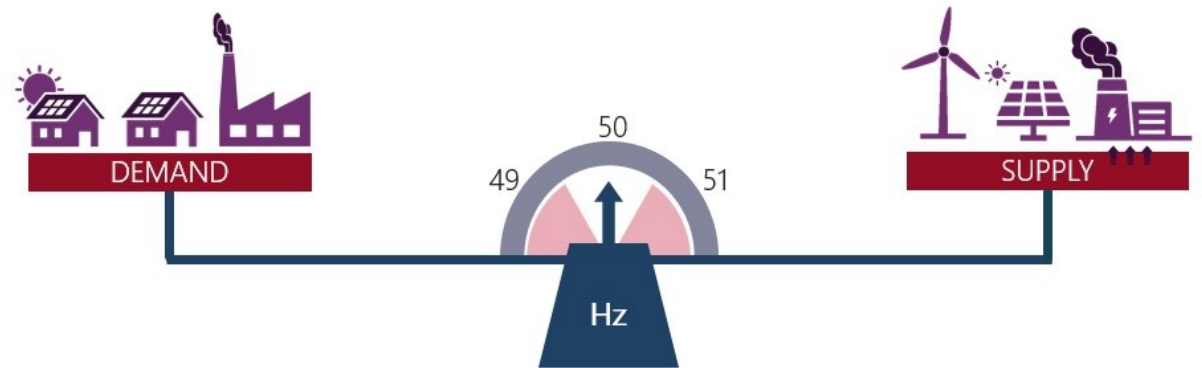
- Grid Frequency is an important measure of grid stability



<https://aemo.com.au/learn/energy-explained/energy-101/energy-explained-frequency>

Grid Frequency

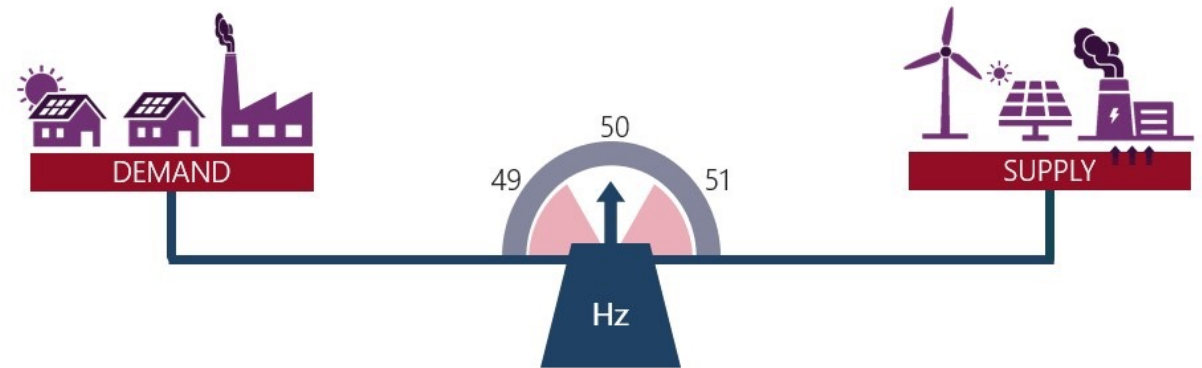
- Grid Frequency is an important measure of grid stability
- Coupled to power balance



<https://aemo.com.au/learn/energy-explained/energy-101/energy-explained-frequency>

Grid Frequency

- Grid Frequency is an important measure of grid stability
- Coupled to power balance
- What happens in case of imbalance?



<https://aemo.com.au/learn/energy-explained/energy-101/energy-explained-frequency>

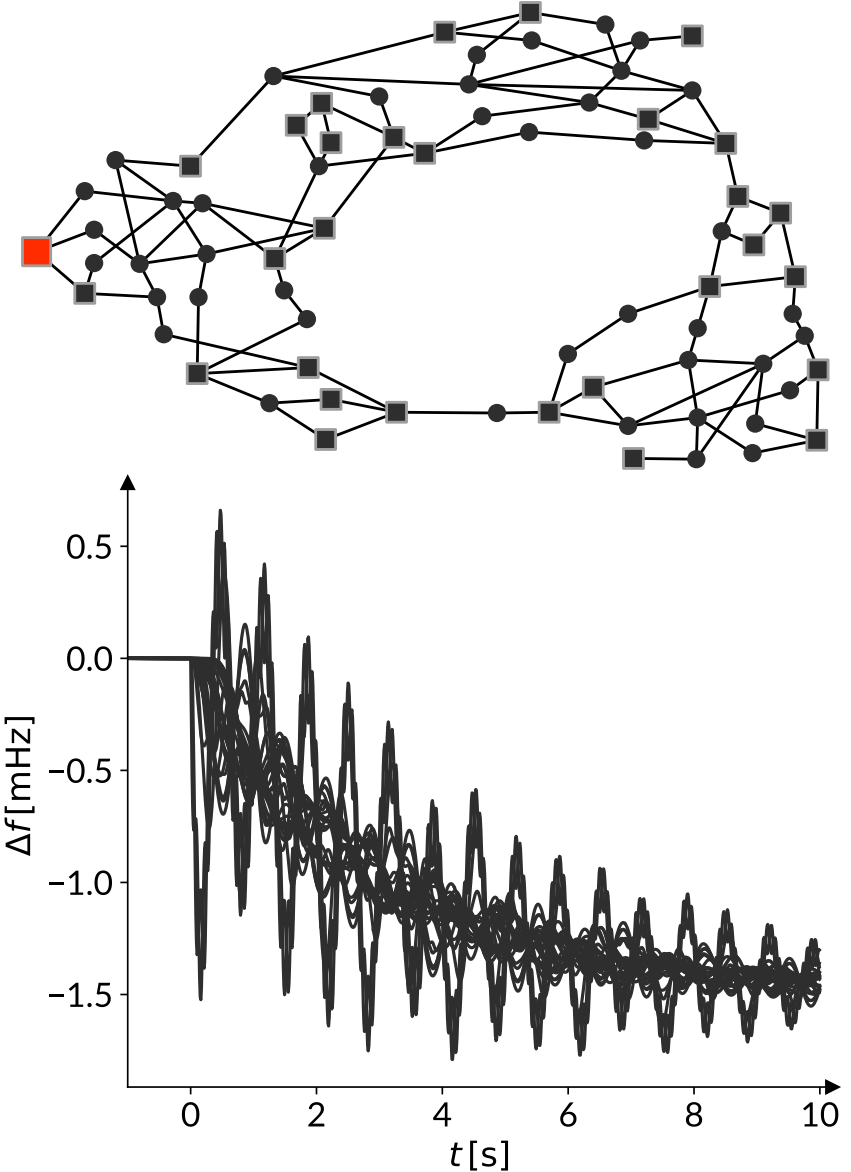
Swing Equations

$$m_i \dot{\omega}_i + d_i \omega_i = P_i - \sum_j b_{ij} \sin(\theta_i - \theta_j)$$
$$d_i \omega_i = P_i - \sum_j b_{ij} \sin(\theta_i - \theta_j)$$

When linearized around a fixed point:

$$\mathbf{M} \dot{\omega} + \mathbf{D} \omega = \mathbf{P} - \mathbf{L} \theta$$

$\mathbf{L}$ captures network structure



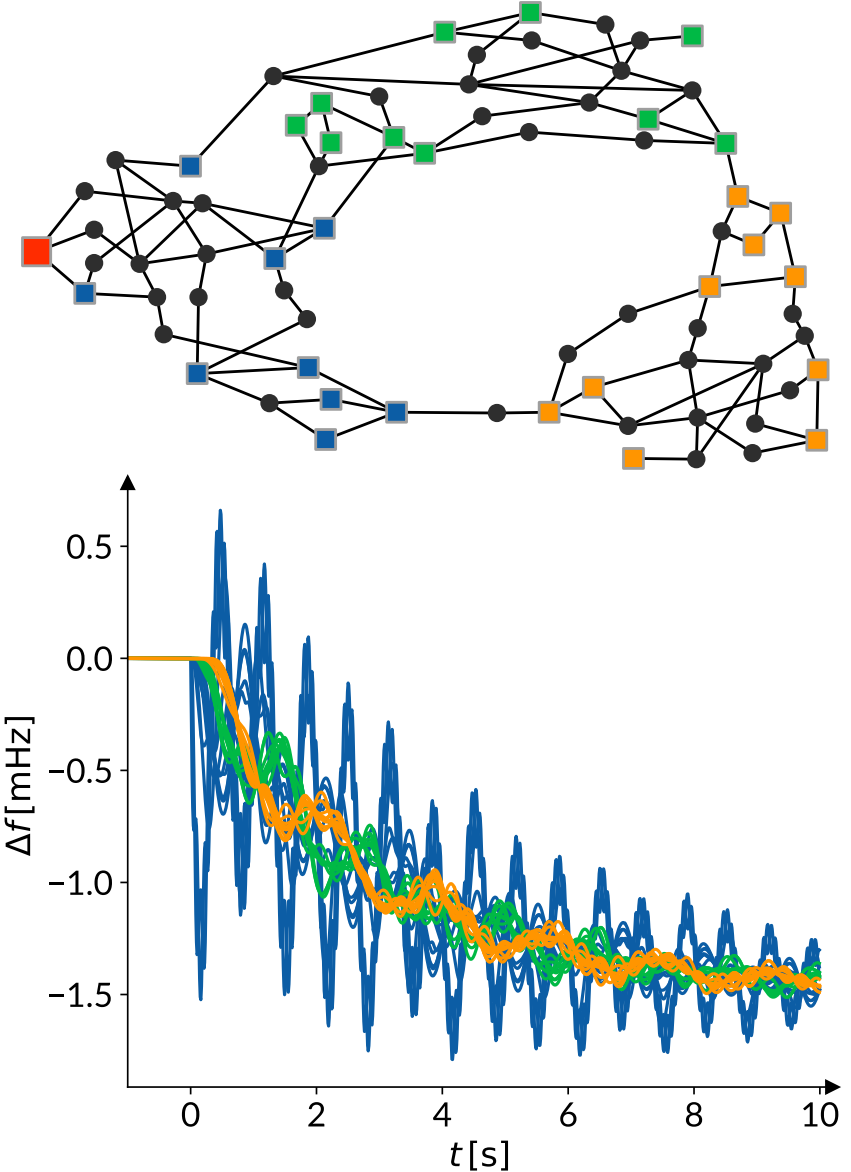
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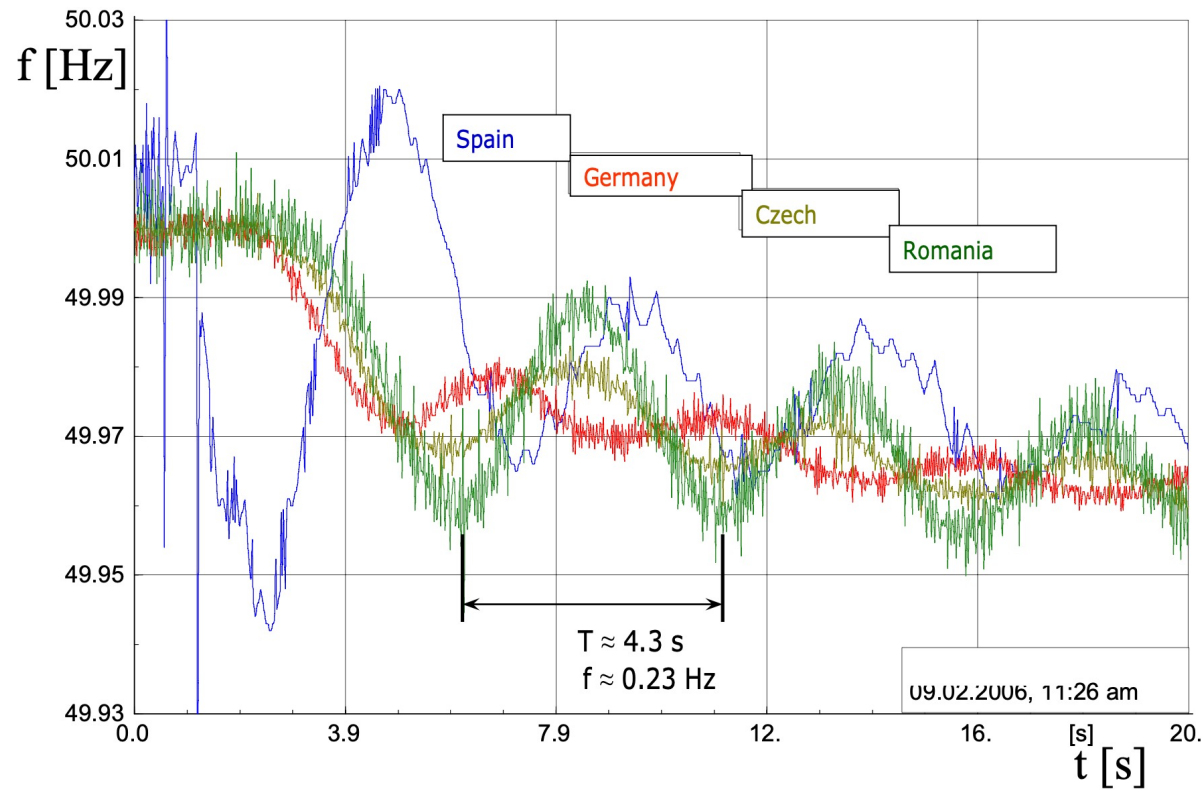
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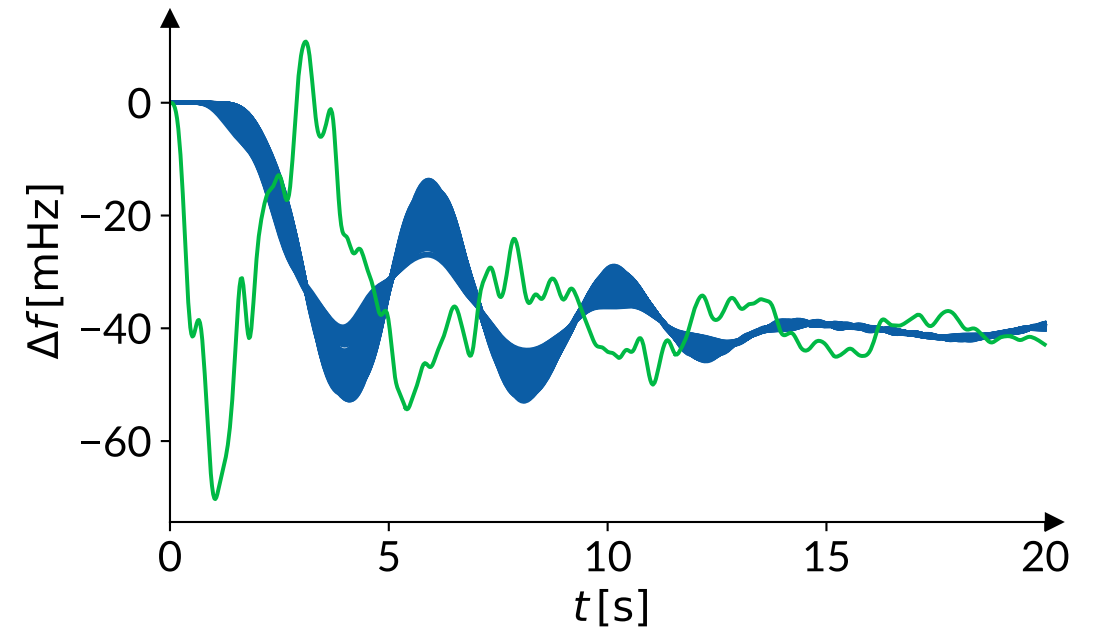
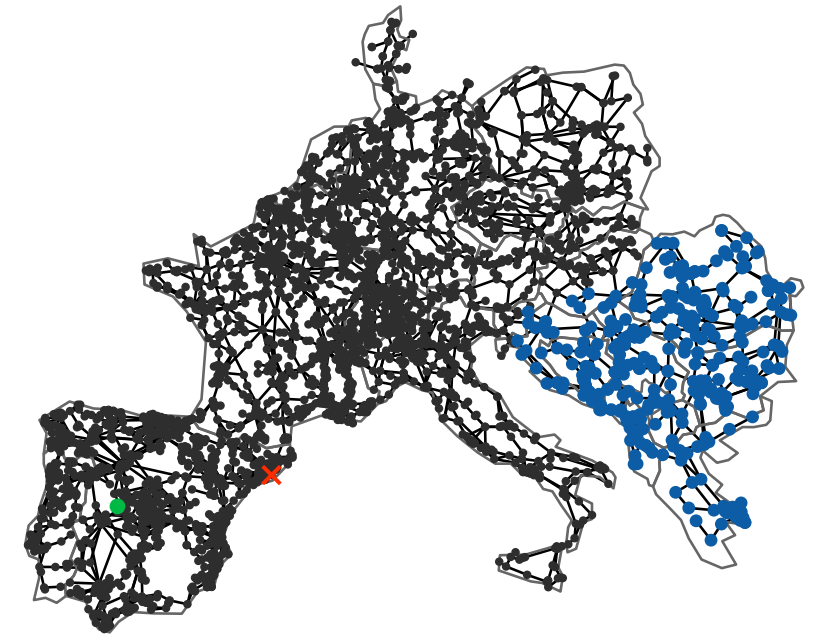
$\mathbf{L}$ captures network structure



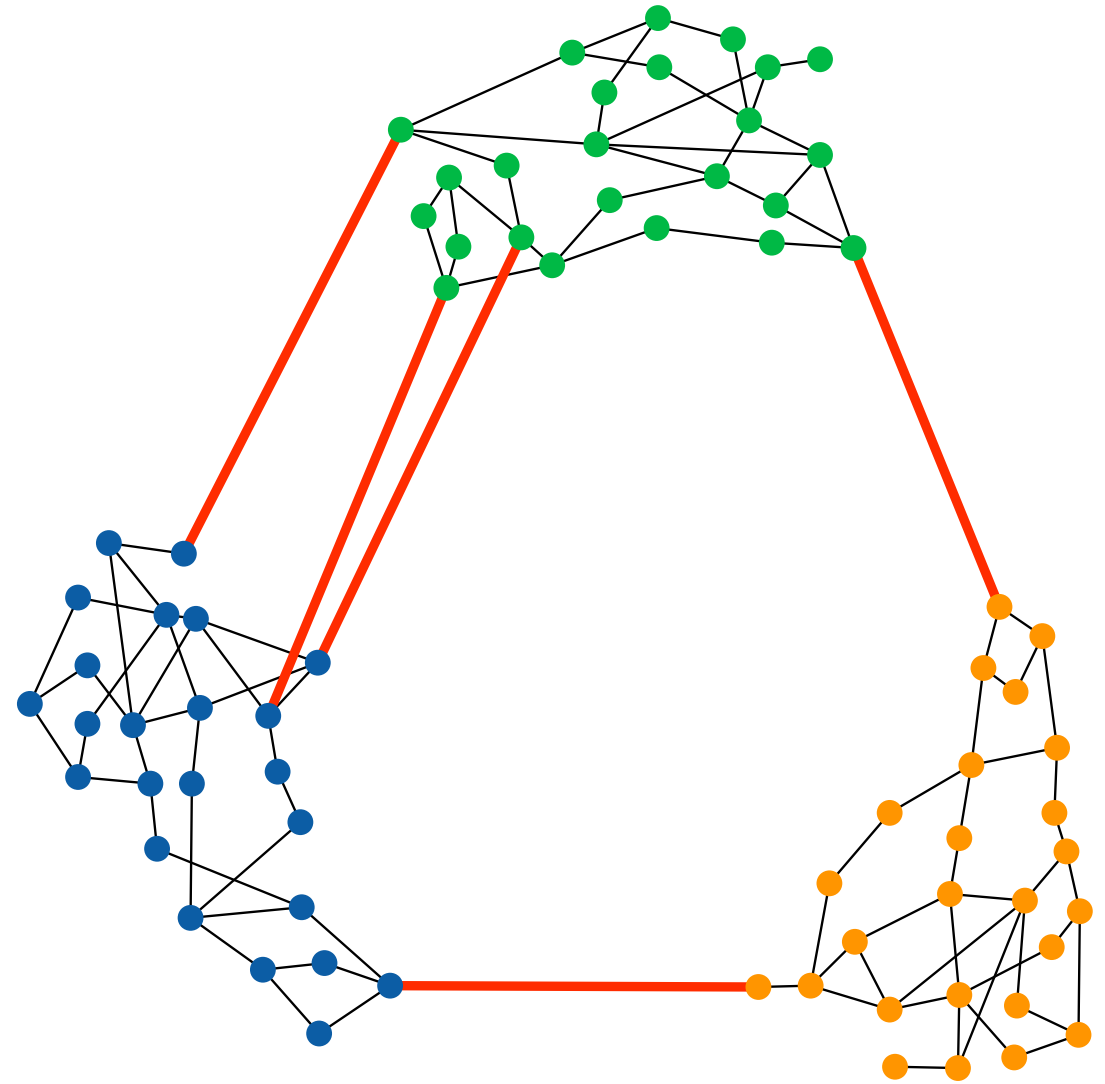
Larger Grids



Al-Ali et al. – 17th Power Systems Computation
Conference 2011

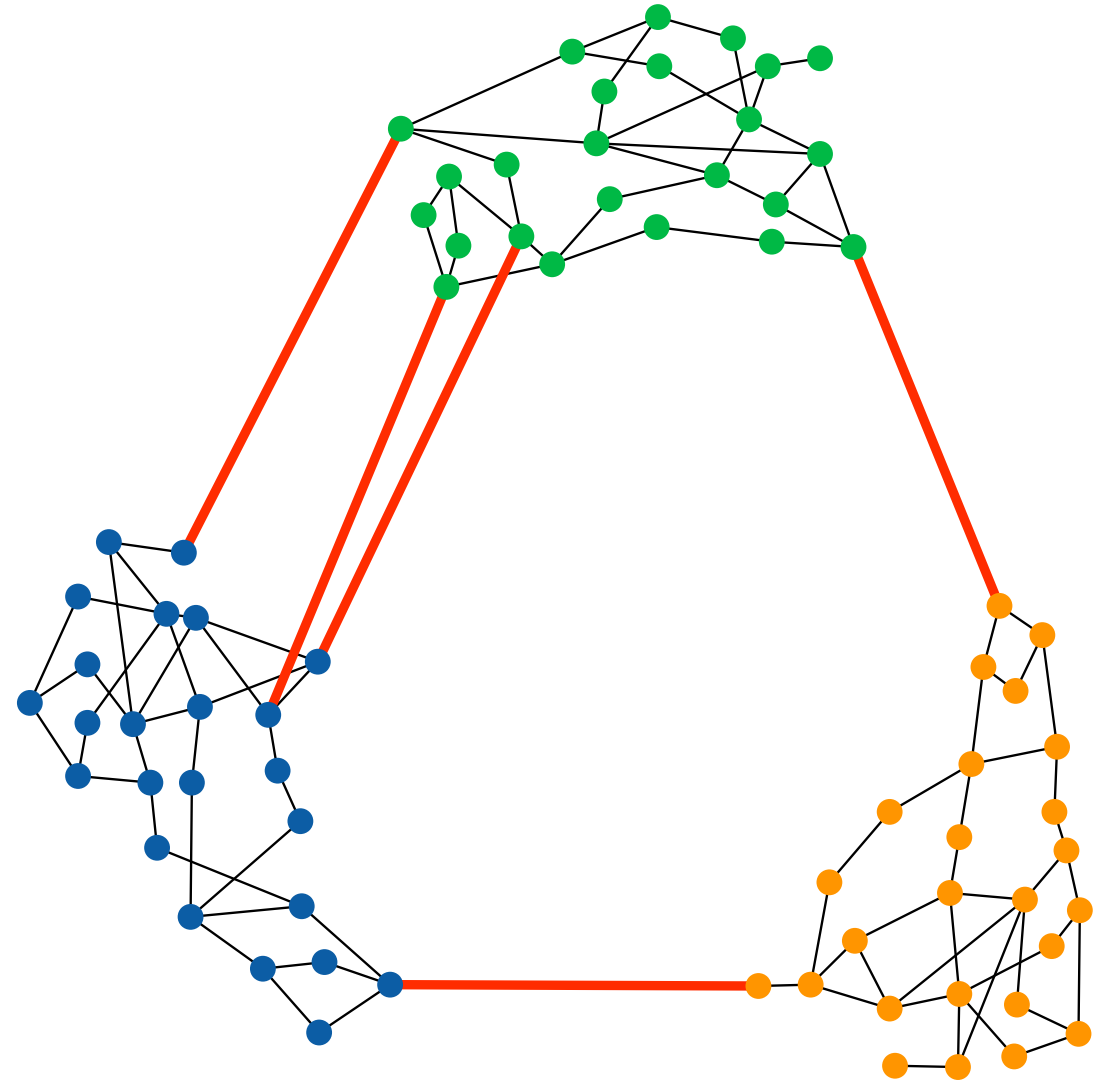


Perturbation Theory



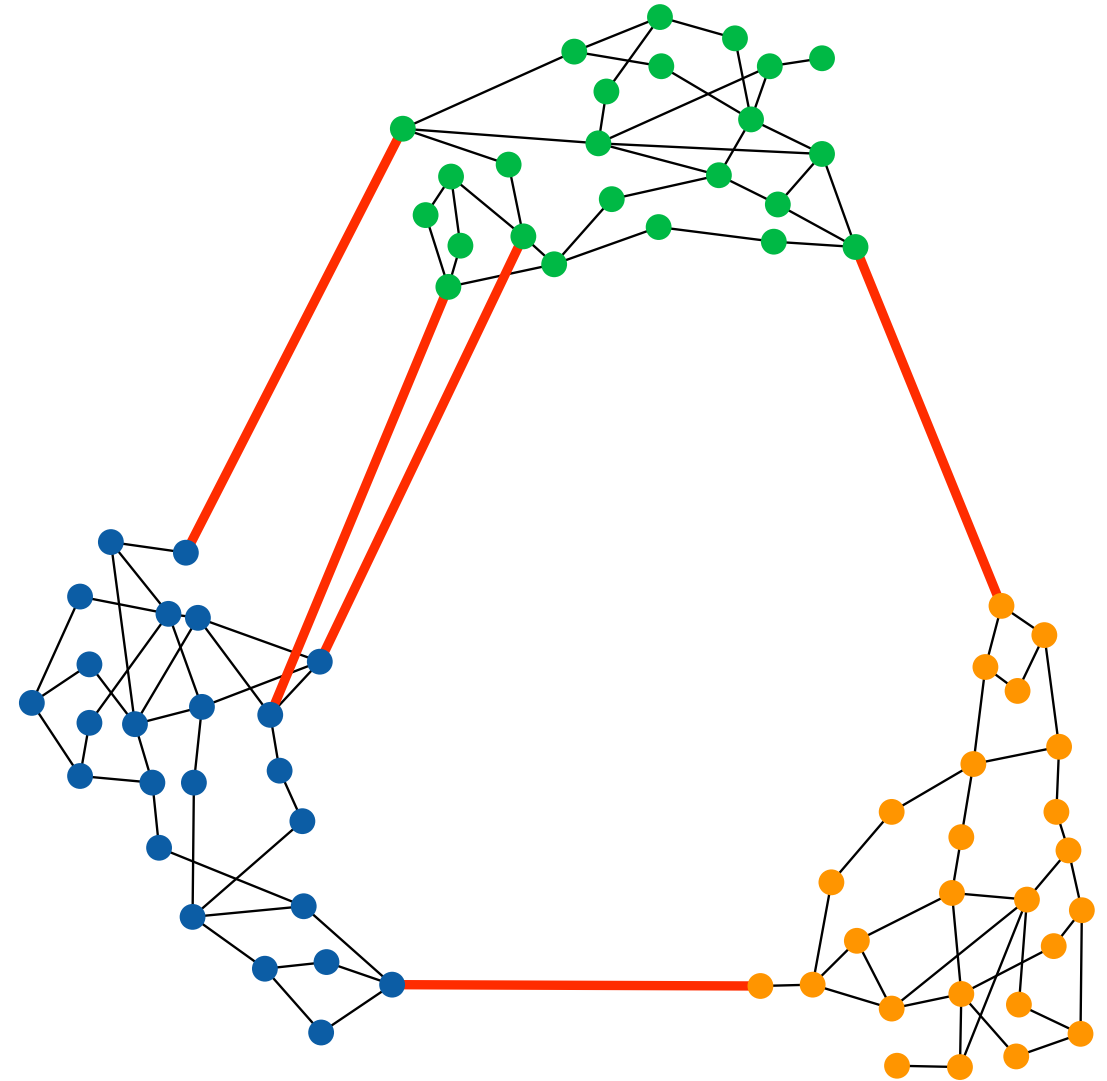
Perturbation Theory

- Start with disconnected areas



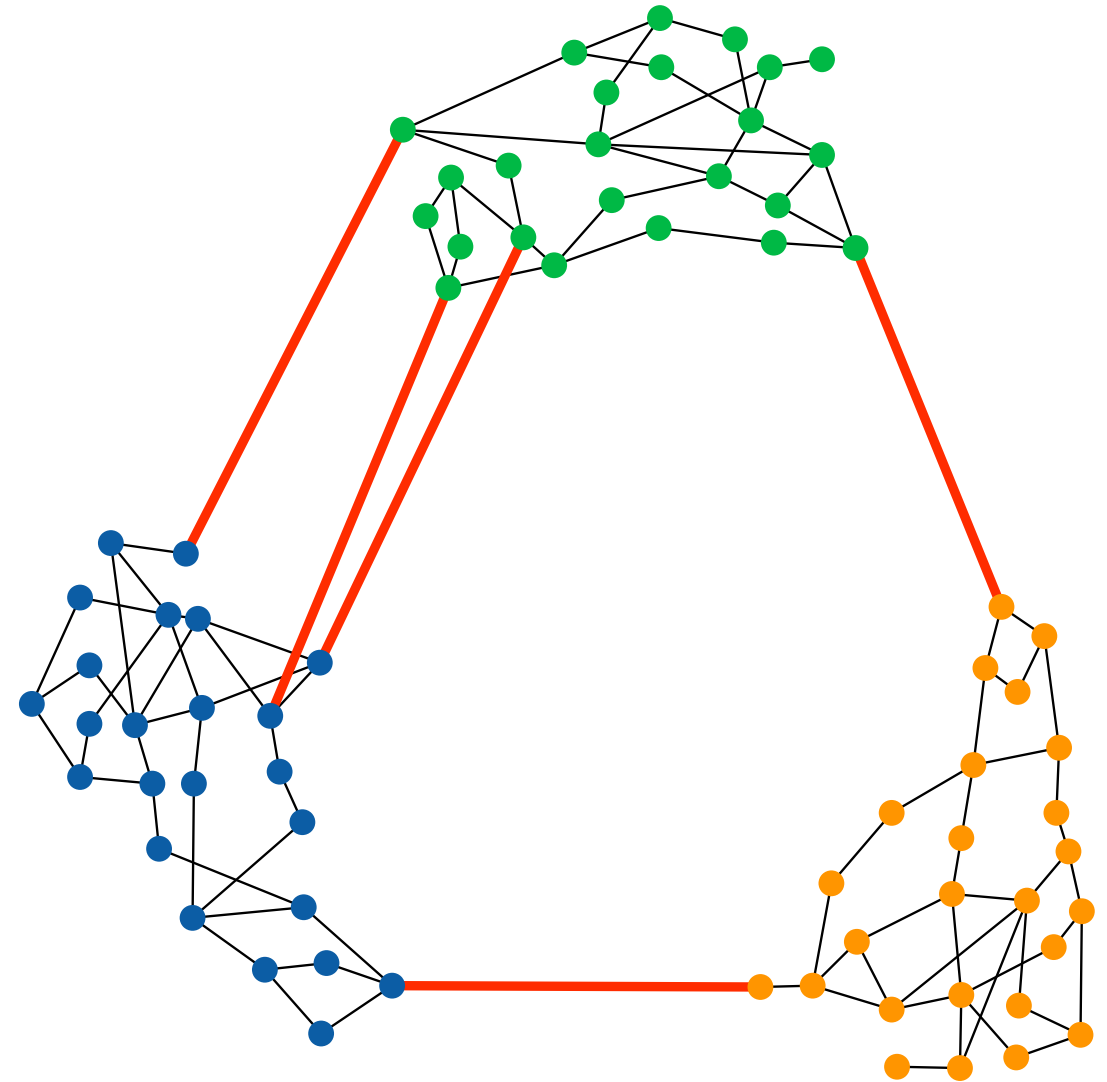
Perturbation Theory

- Start with disconnected areas
- Connections are perturbations



Perturbation Theory

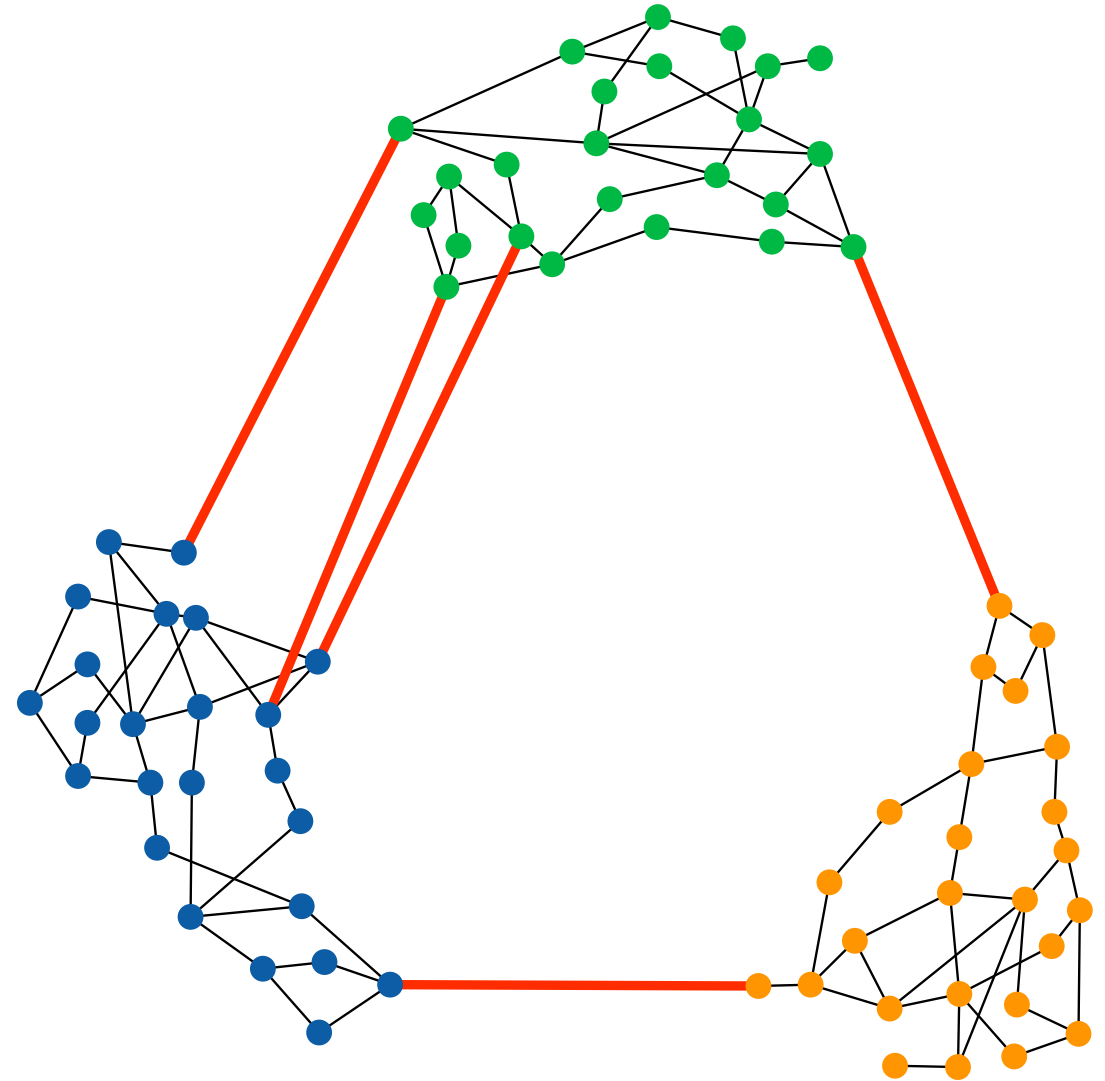
- Start with disconnected areas
- Connections are perturbations
- How do they interact?



Perturbation Theory

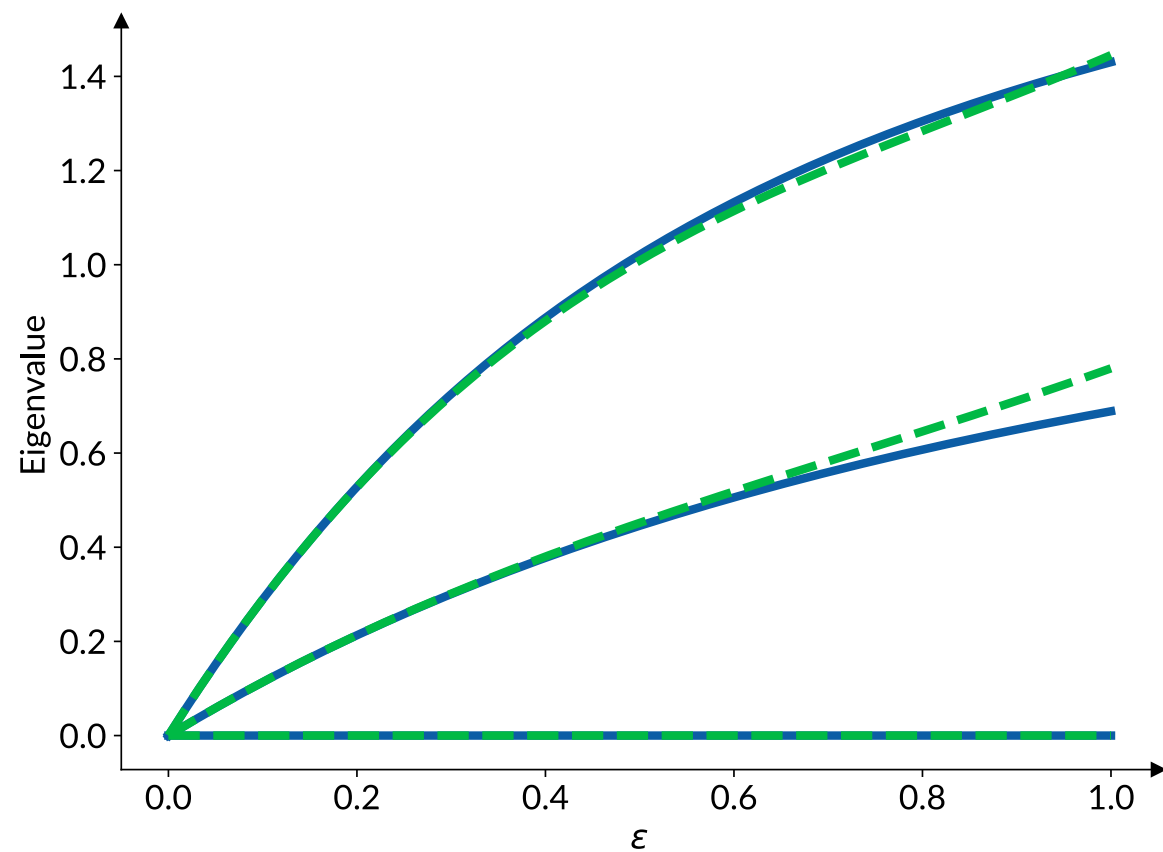
- Start with disconnected areas
- Connections are perturbations
- How do they interact?

$$\mathbf{L} = \begin{bmatrix} \mathbf{L}_1 & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{L}_2 & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{L}_3 \end{bmatrix} + \varepsilon \mathbf{L}_i$$

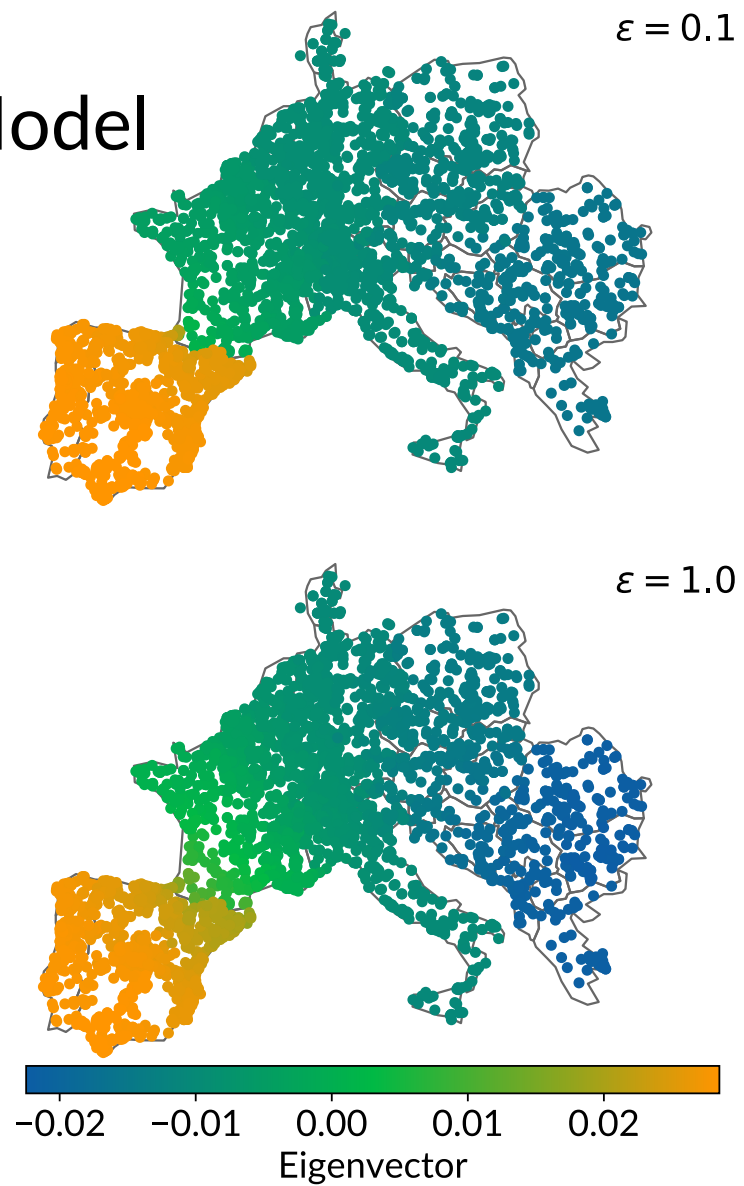


Results

3 Areas



European Model

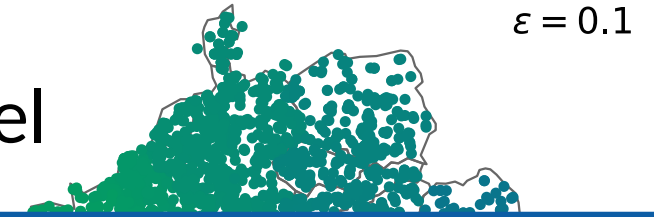


Results

3 Areas



European Model



2021 60th IEEE Conference on Decision and Control (CDC)
December 13-15, 2021. Austin, Texas

Matrix Perturbation Theory of Inter-Area Oscillations

J. Fritzsche, M. Tyloo, and Ph. Jacquod

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Long Wavelength Coherency in Well Connected Electric Power Networks

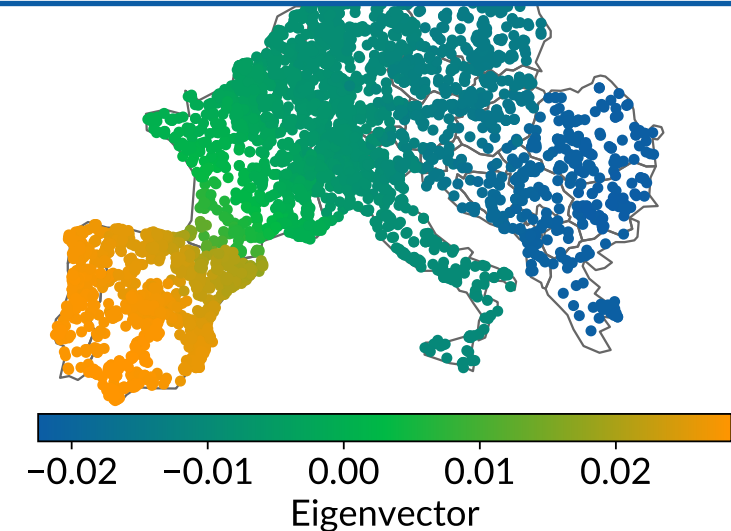
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School of Engineering, University of Applied Sciences of Western Switzerland—HES-SO, 1951 Sion, Switzerland

Corresponding author: Julian Fritzsche (julian.fritzsche@etu.unige.ch)

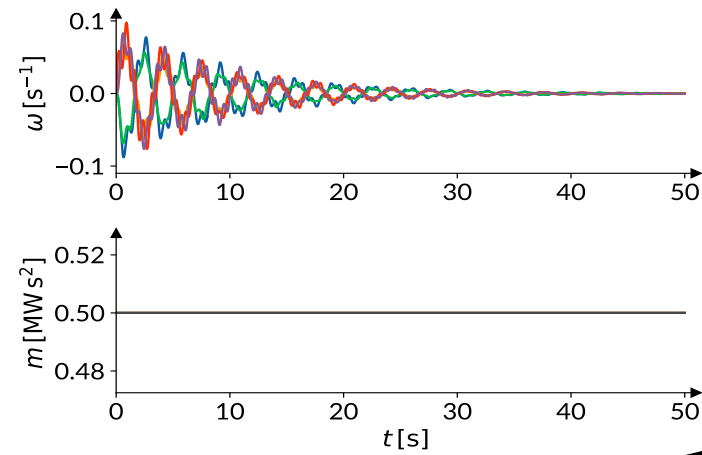
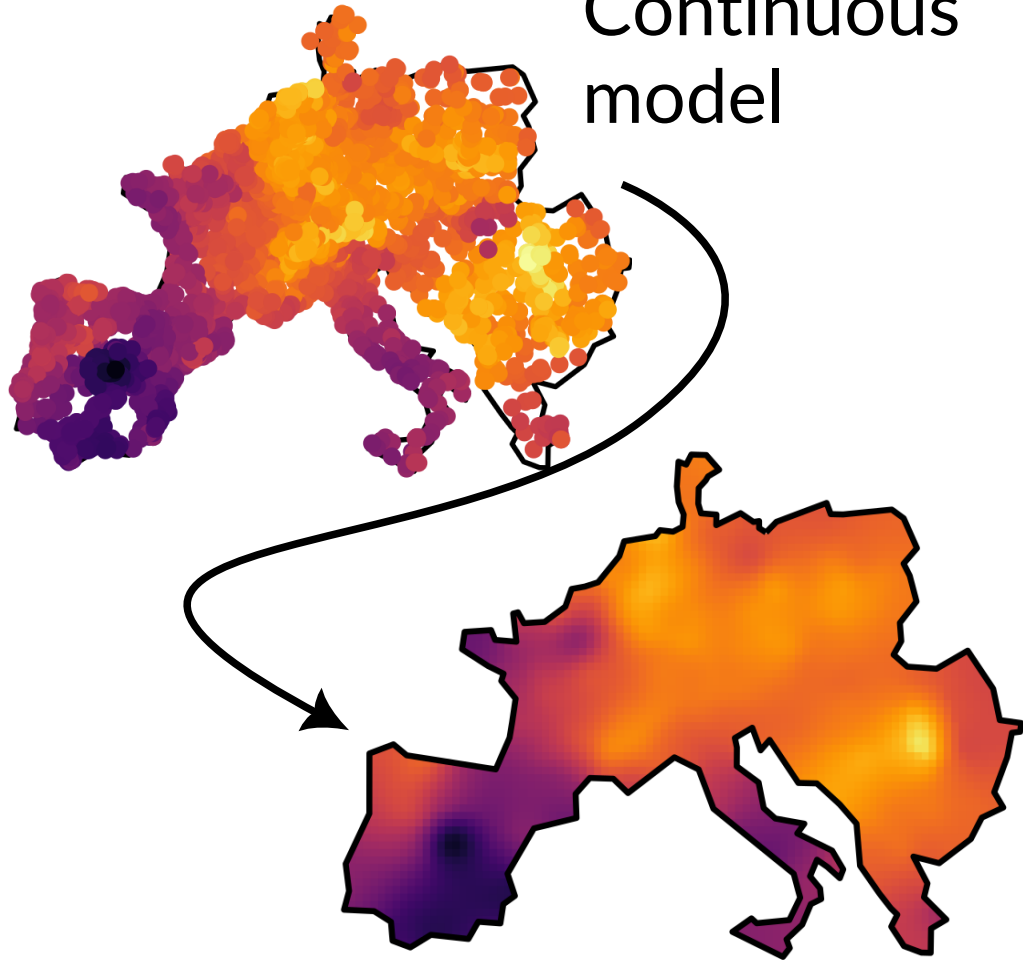
This work was supported by the Swiss National Science Foundation under Grant 200020_182050.

a number of conditions under which they occur and how to damp these

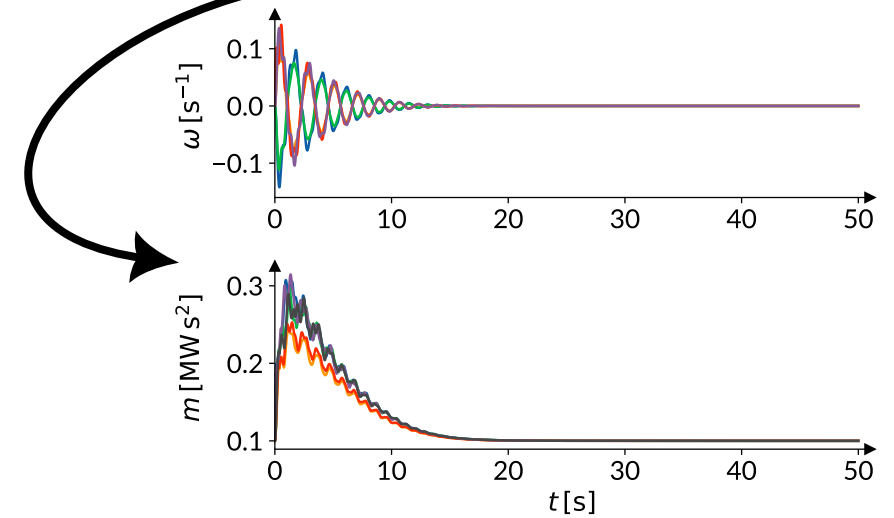


Outlook

Continuous
model

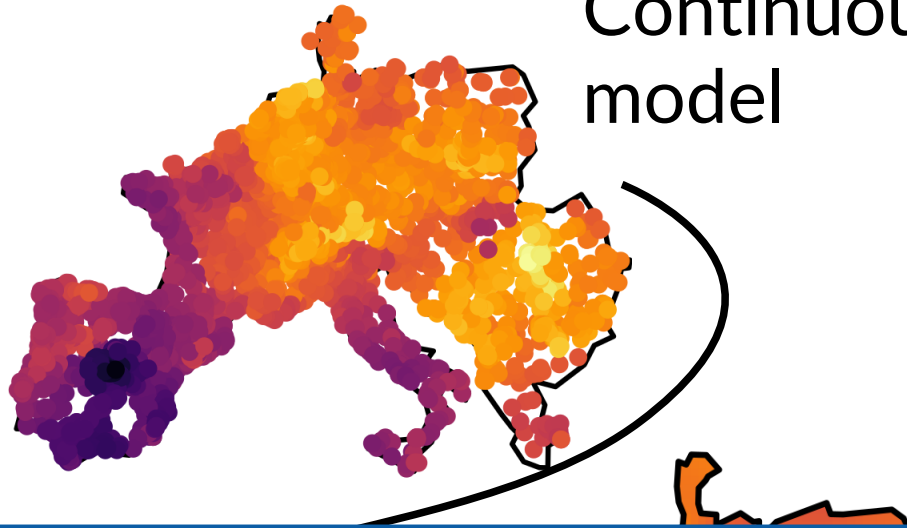


Adaptive
inertia



Outlook

Continuous
model



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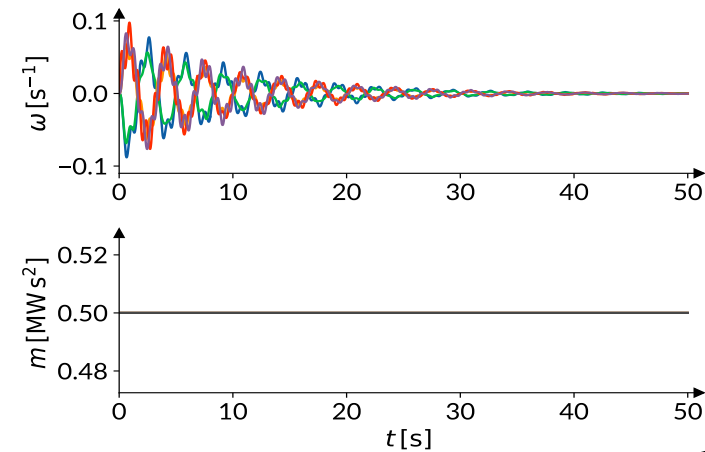
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Toward Model Reduction for Power System Transients With Physics-Informed PDE

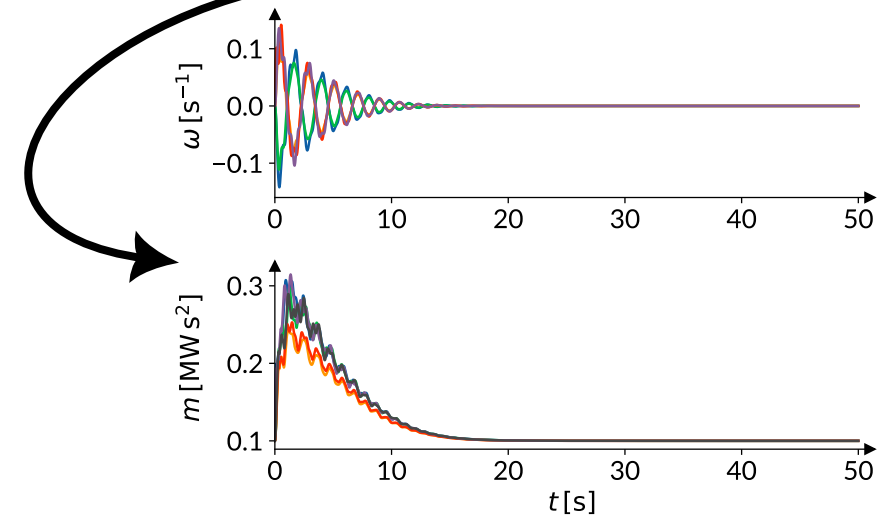
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PHILIPPE JACQUOD^{2,3}, (Member, IEEE), AND
MICHAEL CHERTKOV¹, (Senior Member, IEEE)

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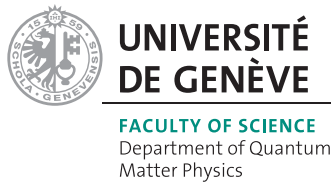
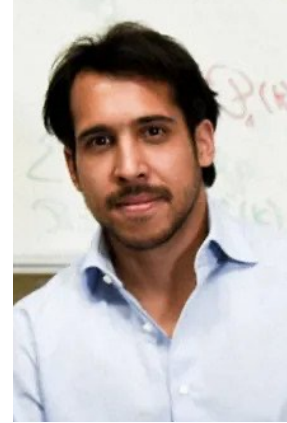
²School of Applied Sciences, University of Applied Sciences of Western Switzerland – HES SO – 1050 Sion, Switzerland



Adaptive
inertia



Group and Collaborators



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