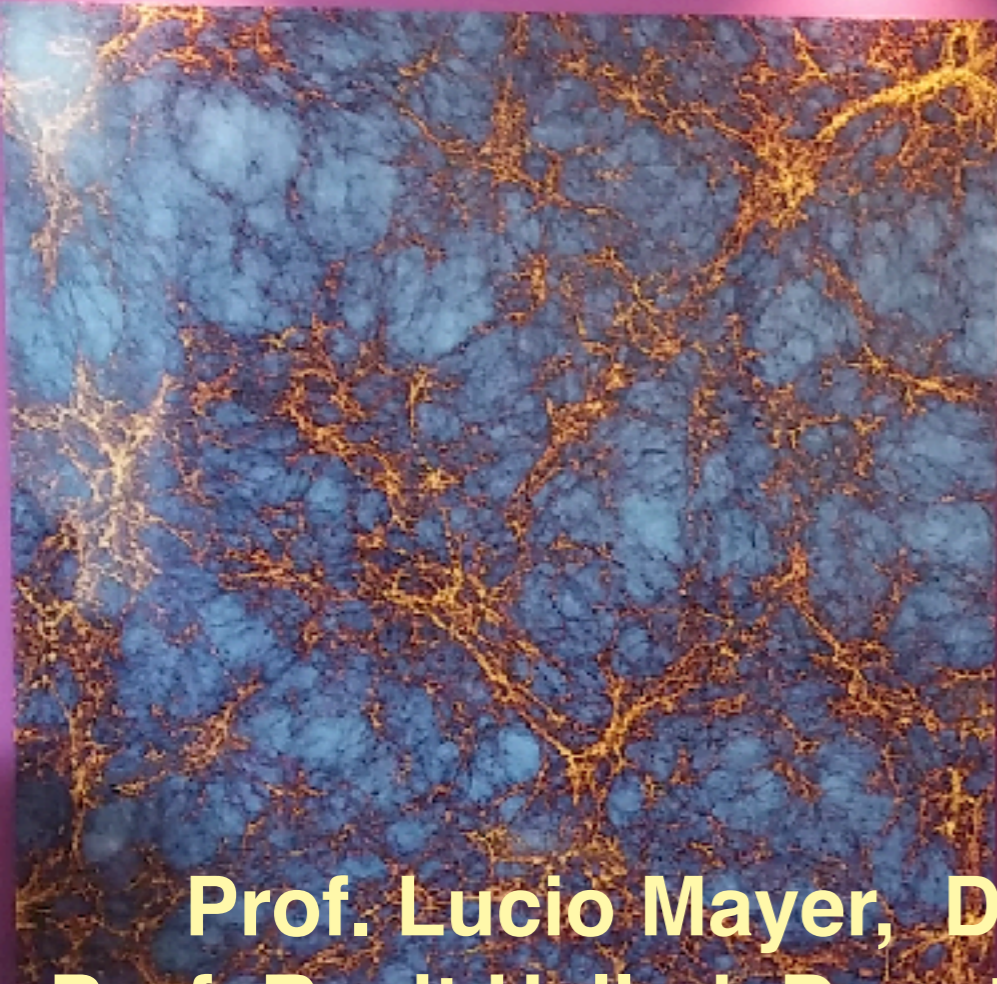


# Institute for Computational Science (ICS) Center for Theoretical Astrophysics and Cosmology



**Prof. Lucio Mayer, Director ICS**  
**Prof. Ravit Helled, Deputy Director ICS**

**As of September 2022 ICS hosts 11 professors, 2 permanent research staff members, and 42 among PhD Students and Postdoctoral Researchers**

# Main research areas with group leaders

## I. Supercomputer simulations for astrophysics and cosmology

(Mayer, Stadel, Feldmann, Schneider)

**Development of major parallel supercomputer codes  
employed by international community**

(PKDGRAV3, GASOLINE2/ChaNGa, GENGA, GIZMO, SPH-EXA – collaboration  
with University of Basel, University of Washington, Caltech,  
McMaster University, University of Oslo, UC Santa Cruz, Princeton University)

*Focus applications: cosmological structure and galaxy formation,  
(super) massive black holes growth and evolution*

## II. Theoretical Cosmology

(Yoo, Adamek, Schneider). **Relativistic effects in structure formation**

## III. Black Hole and Gravitational Wave Astrophysics

(Mayer) - **Supermassive Black Hole Binaries and Waveform Physics**

## IV. Planetary Science

(Helled, Mayer, Moore, Stadel, Mazzola) - **Interiors and Formation**

## V. Data Science for Natural Sciences

(Wegner, Feldmann)

# ICS researchers have strong Involvement in LISA Consortium and LISA Astrophysics Working Group (WG)



**Current group members involved in GW research:**

**Pedro Capelo, Andrea Derdzinski (Postdocs), Lorenz Zwick, Mudit Garg, Lara Bohnenblust, Noemi Fabri (PhD students), Simone Pacuraru (exchange Msc student with Universita' Milano-Bicocca)**

**Affiliate Group Member: Prof. Harald Ita + postdoc expert  
in scattering amplitude calculations  
(in hiring phase)**

**() LISA Astrophysics Working Group leadership: Mayer Co-Chair since 2018**

**()LISA Astrophysics White Paper: 3 coordinators from ICS**

**()Sub-Workpackage “Massive BHs” Group Leader: Pedro Capelo**

**()Contributors to LISA Red Book (Mayer and Capelo for MBHs, Zwick and Derdzinski for EMRIs/IMRIs)**

**() LISA Astro WG collaborative projects: leadership of new “DiscIMRI” code comparison**

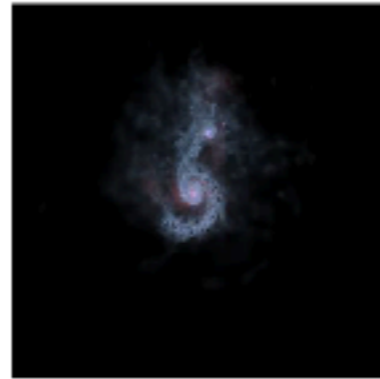
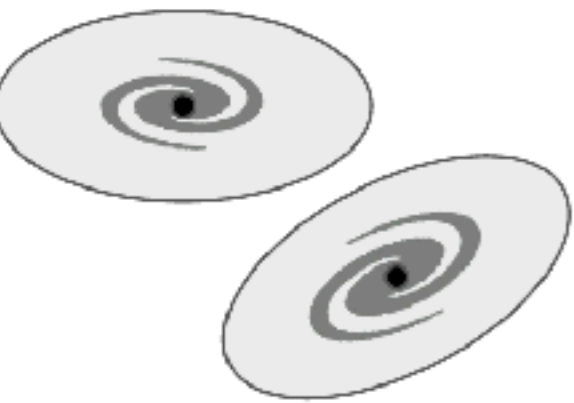
# Research topics in GW science

- 1. Multi-scale simulations of LISA massive black hole binaries in Galactic nuclei (from kpc to  $10^{-2}$  pc scales) w/newtonian hydrodynamics, post-newtonian gravity (in some cases)**
- 2. Formation of the seeds of LISA massive black holes at high redshift** (*recall LISA has, in principle, the power to distinguish between different BH seed models via even rate distribution as a function of redshift*). **Analytical models and simulations**
- 3. Simulations of early in-spiral phases of IMRIs embedded in gaseous accretion disk --> evolution of orbital parameters and disk-driven torques as perturbations to waveforms**
- 4. (Semi)analytical models of waveform perturbations due to environment and their detectability Study using toy model (eg “Dirty Waveforms” – Zwick et al. 2022, and Garg et al. 2022)**
- 5. In-situ generation of IMRIs, EMRIs and stellar BH sources in accretion disks around SMBHs (with semi-analytical models and hydro+MHD simulations)**
- 6. Scattering amplitude methods borrowed from QCD as new tools to construct accurate waveforms for highly eccentric sources in the PM approximation**

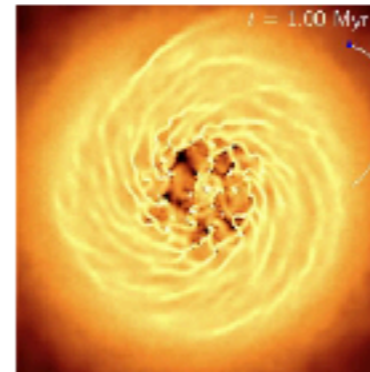
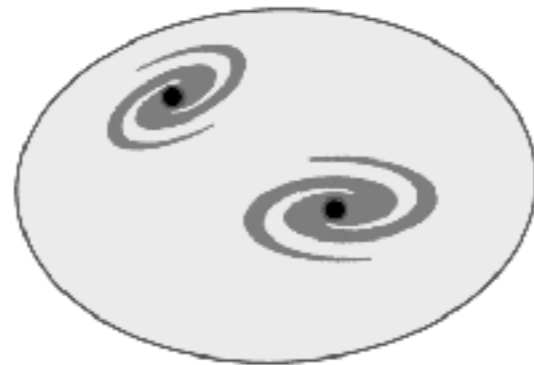
# The four key stages of MBH binary evolution until onset of GW emission: multi-scale numerical simulations



Credit: Lupi et al. (2019)

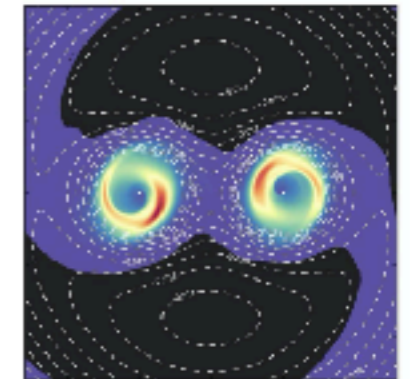


Credit: Capelo et al. (2015)



Credit: Souza Lima et al. (2017)

**Circumnuclear gas disk (CND) stage**



Credit: Bowen et al. 2017

**Circumbinary gas disk stage**



Mpcs:  
The large scale structure

Influence of the large scale environment on: black hole seeding, frequency of mergers, galaxy transformation

1-100s kpcs:  
Galaxy interactions/merger

Details of the merger have influence on: black hole growth via gas accretion, formation of a black hole binary, galaxy transformation

1-10s pc:  
Formation of a bound binary

The host properties have influence on: hardening of the binary, accretion episodes  
**Degree of clumpiness of gas disk matters for orbital evolution, accretion etc.**

<1 pc:  
Hardening of the binary

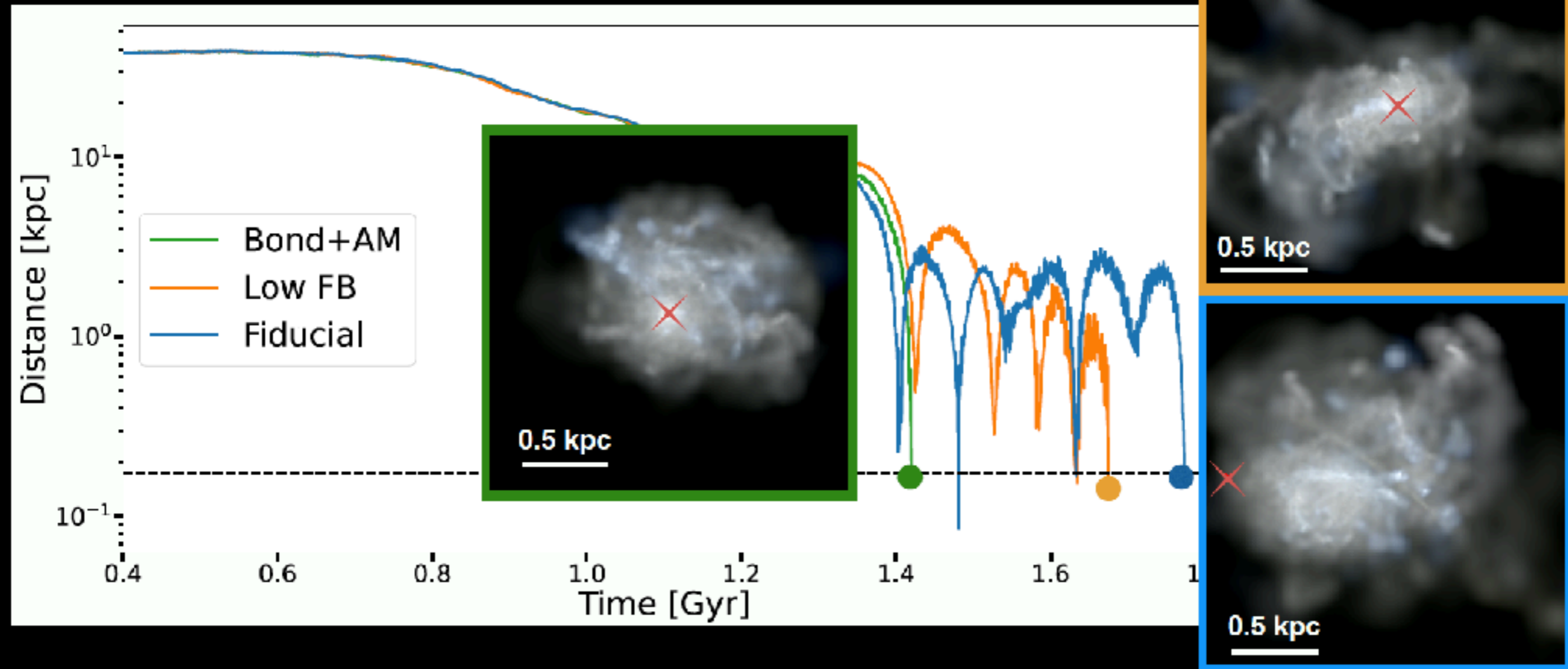
The host properties have influence on: timescale of hardening  
Effect of circumbinary disc  
Three-body interactions (hyper-velocity stars)

From LISA Astrophysics White Paper

# Cosmological hydro simulations of galaxies with embedded massive BHs in the LISA band

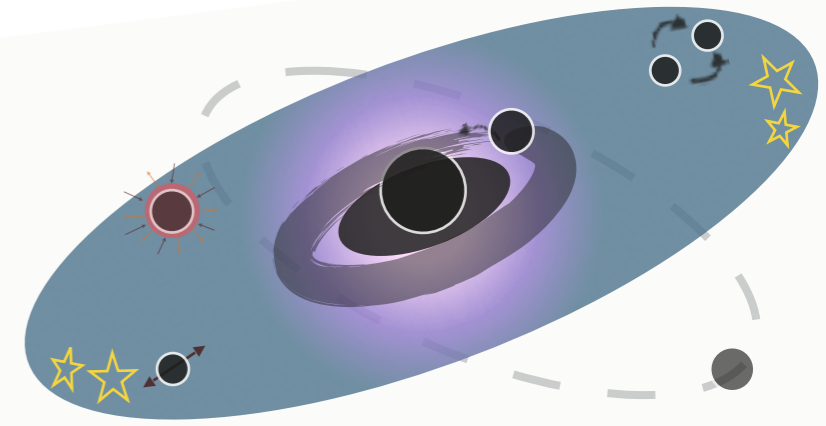
Dynamical Evolution of Massive Black Hole Pairs

The BH merger timescale is affected by the properties of the merging galaxies



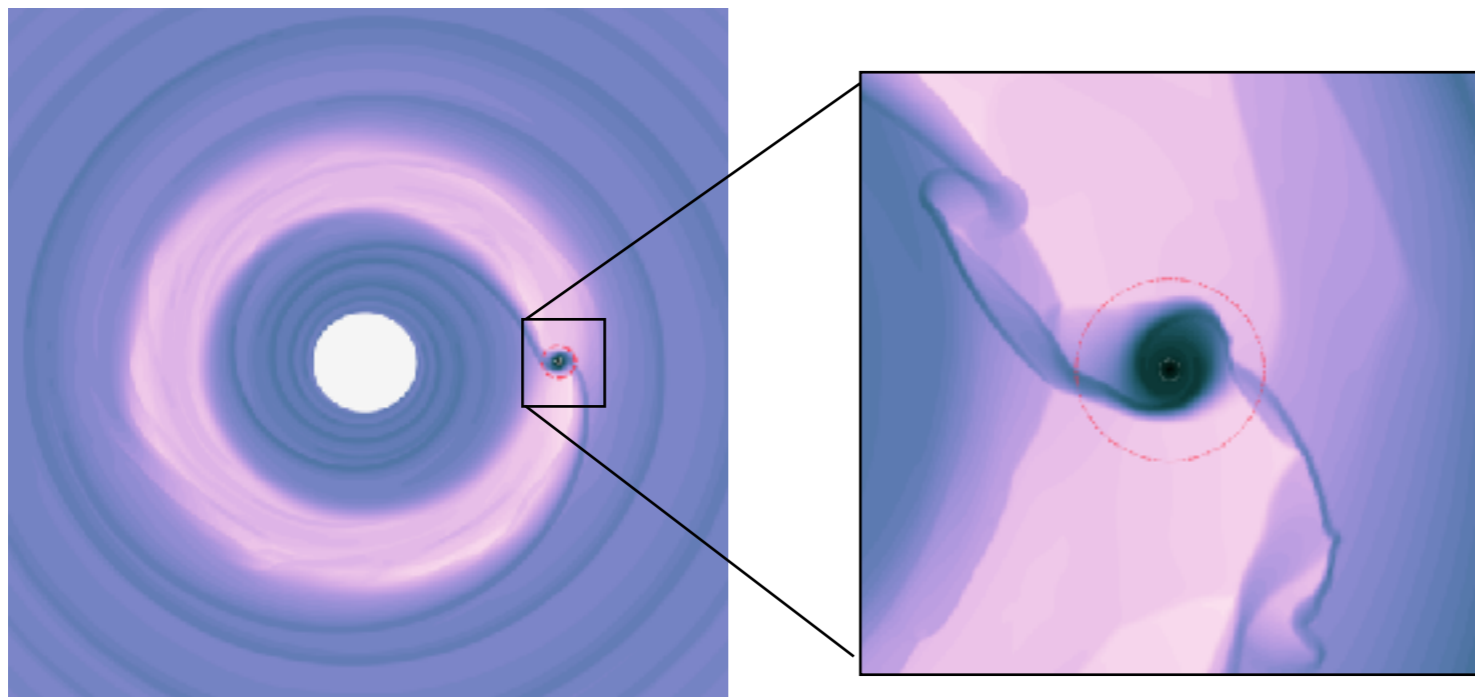
Above: same dwarf galaxy merger with different models for radiation feedback by massive black hole at center (Tremmel et al. in preparation)

# Hydrodynamical simulations of unequal mass BHs and EMRIs/IMRIs in accretion disks

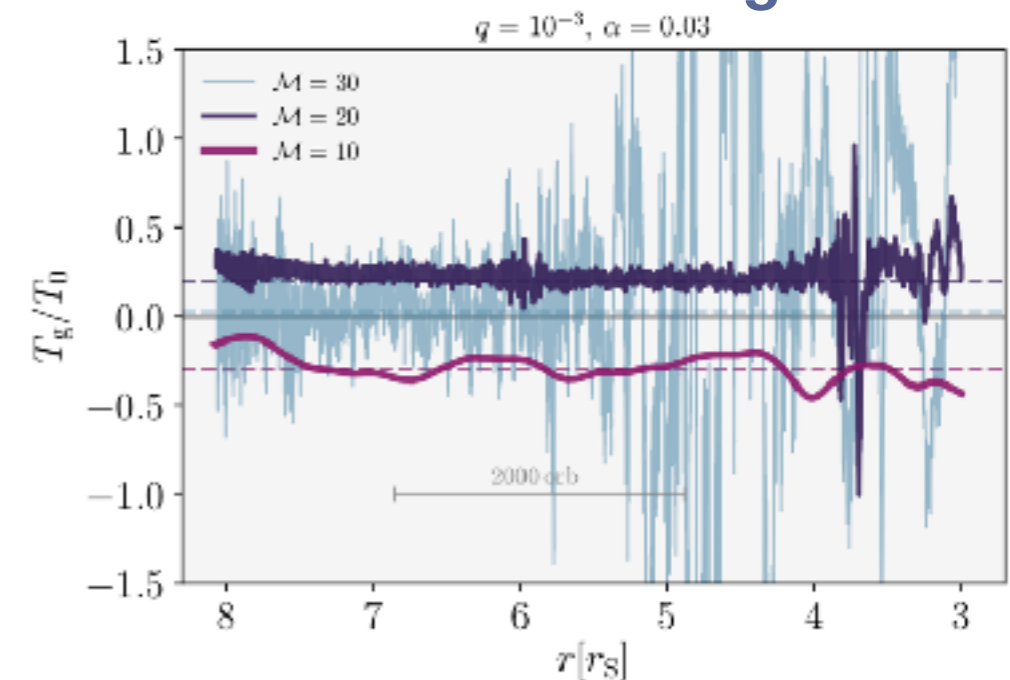


- Gas interaction determines rates, orbital properties, and evolution *during* GW early in-spiral phase
- EMRIs produced via in-situ star formation in massive AGN disks can outnumber the conventional EMRI rate in star clusters

Derdzinski & Mayer (2022:arXiv220510382D)  $R_{\text{AGN}} \sim 0.5 - 10 \text{ yr}^{-1} \text{ Gpc}^{-3}$

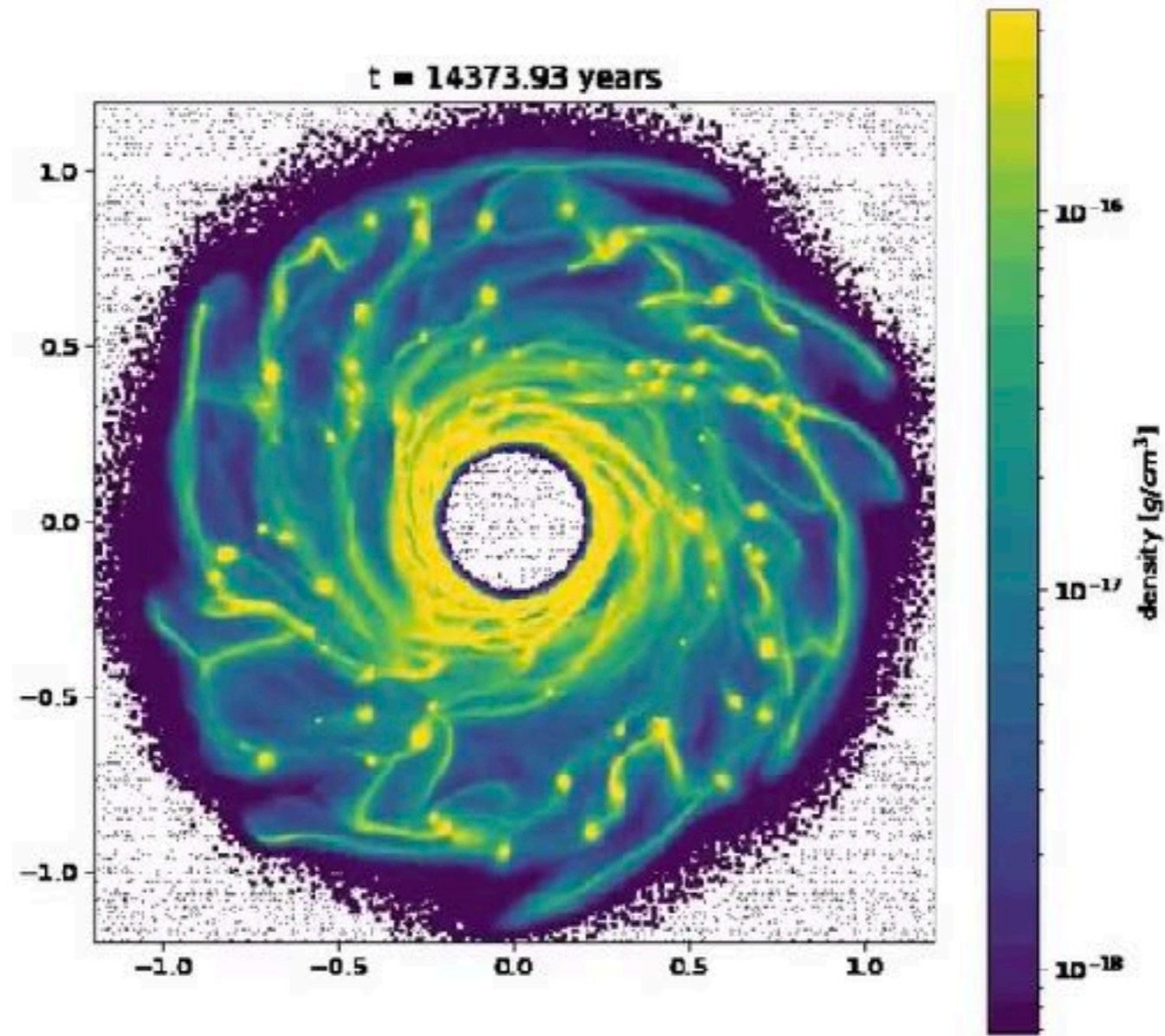


**Torques exerted by gas affect GW signals**



Derdzinski+ 2021

- In-situ population of massive stellar remnants interact with gas and with each other  $\rightarrow$  generation of LISA EMRIs and LIGO/Virgo Stellar BH sources, as well as multi-band sources (IMBHs at the LISA-LIGO interface)
- Binaries as well as unbound encounters/scatterings



3D GIZMO-MFM simulation of a fragmenting accretion disk to study directly the formation and dynamics of population of stellar remnants (simulation by Simona Pacuraru)



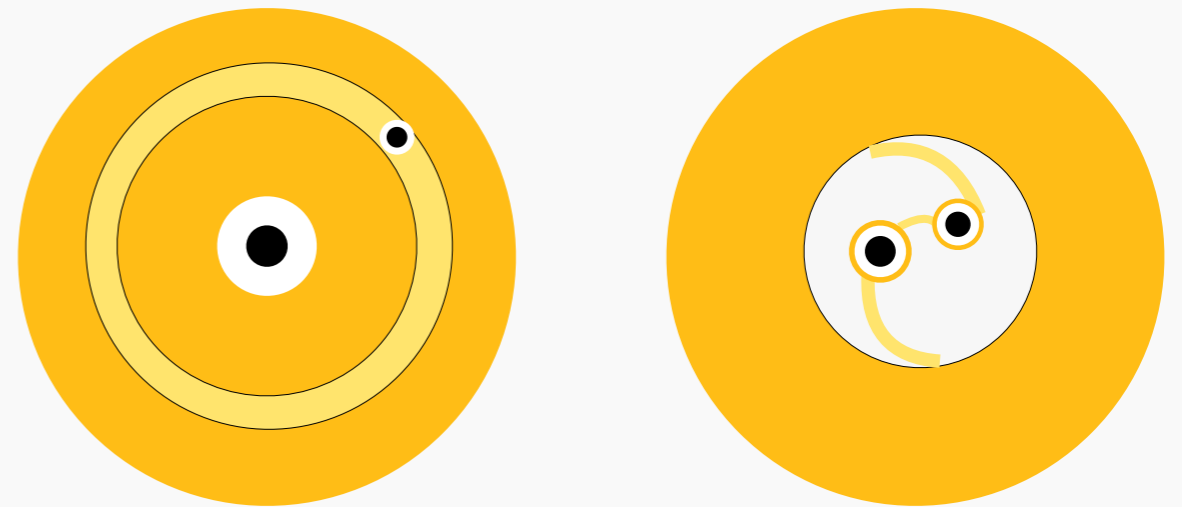
# INTERMEDIATE MASS BLACK HOLES (IMBH) BINARIES: Golden sources for LISA

**Garg et al. 2022, (MNRAS517, 1339):** study of the detectability of environmentally induced phase-shifts in the LISA band

## Features

- Can enter LISA band at separation  $> 100 R_s$
- Can spend  $> 100$  orbits
- Can accumulate SNR
- Can constrain gas physics at small scale

Open Gap/Cavity

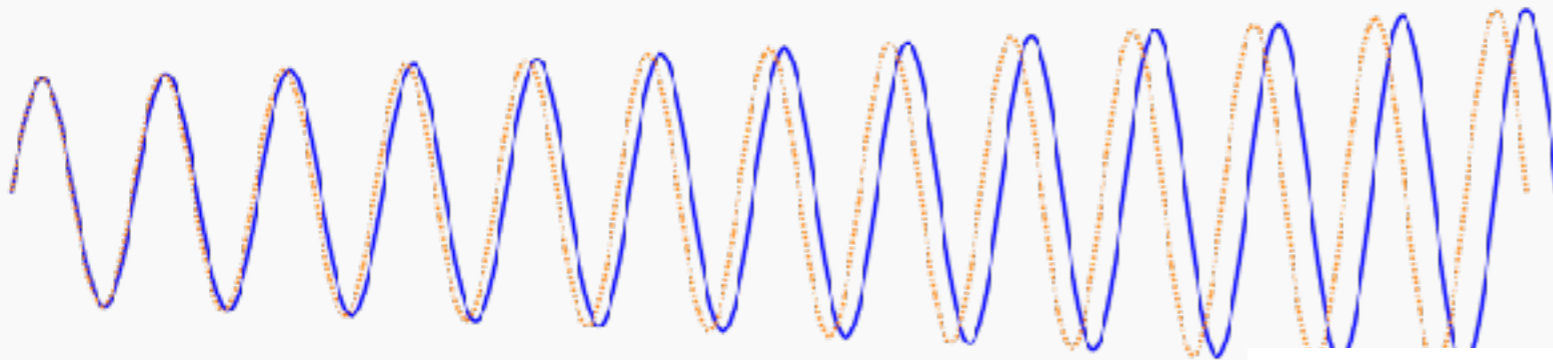


**Simple analytical disk and torque model  
“normalized” with results  
of numerical simulations of  
Derdzinski et al. (2021)**

**Disk torque = (0.1-10) x Viscous torque**

# IMBHB GW waveform carry signature of torques by surrounding gas

— GW waveform in vacuum  
 - - - GW waveform in gas



$$\Phi = 2\pi \int_{r_{\min}}^{r_{\max}} dr \frac{f_r}{\dot{r}}$$

$$\delta\phi = |\Phi(\dot{r}_{\text{GW}}) - \Phi(\dot{r}_{\text{GW}} + \dot{r}_{\text{gas}})| \approx 2\pi \int_{r_{\min}}^{r_{\max}} dr f_r \frac{\dot{r}_{\text{gas}}}{\dot{r}_{\text{GW}}^2}$$

$$\dot{r}_{\text{gas}} \ll \dot{r}_{\text{GW}}$$

BHs decay faster (i.e BHs perform more orbits) than with just GW emission alone  
 —> corresponds to phase change

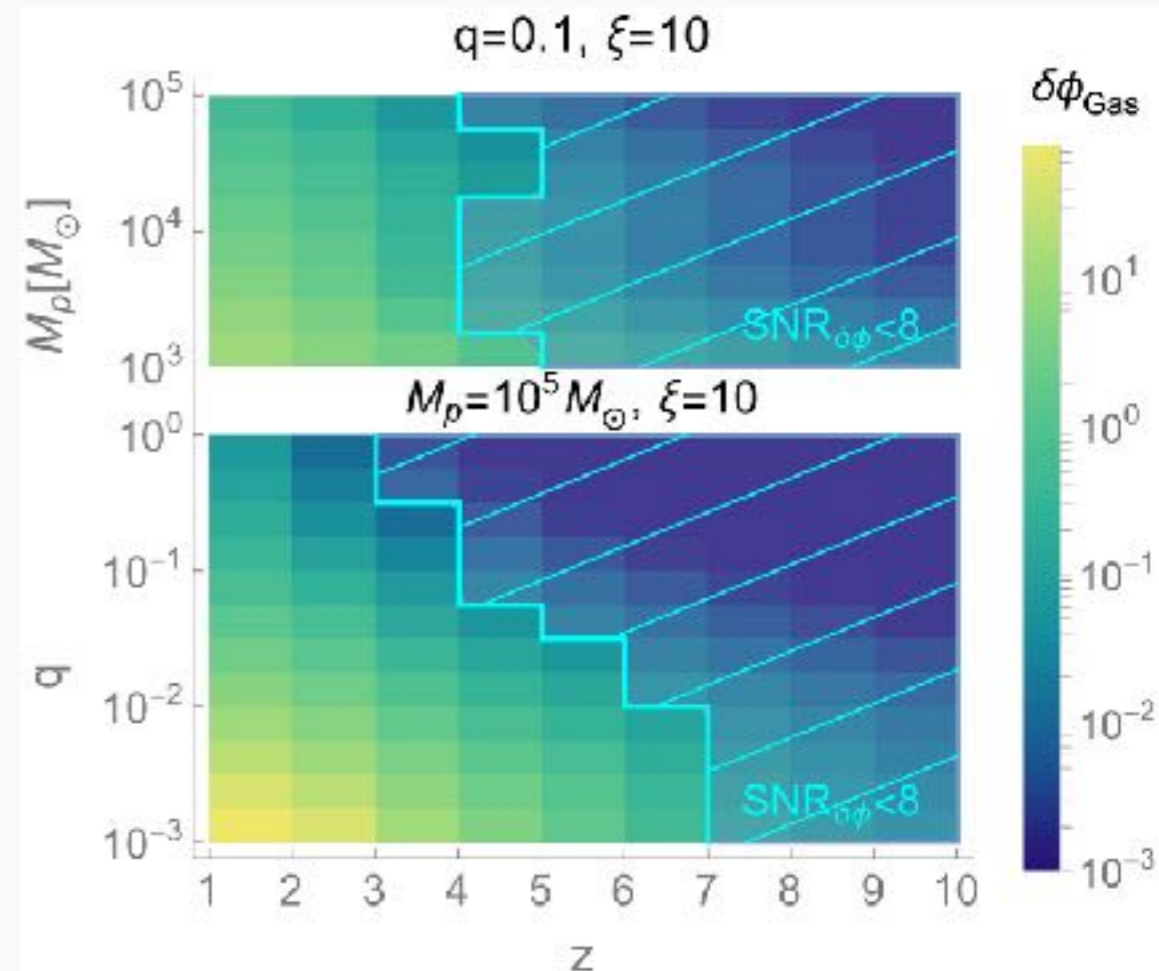
Garg et al.  
 (2022)

**Detectable dephasing**

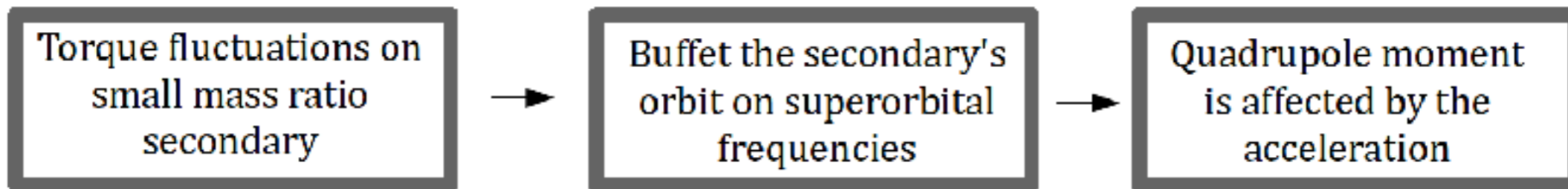
Up to **radians** or **GW cycles**

**See also:**

Kocsis et al. (2011), Yunes et al. (2011),  
 Barausse et al. (2014), Derdzinski et al. (2019, 2021)



The imprint of disk torque fluctuations due to hydro and MHD turbulence as additional harmonics of waveform (also add secular energy drift): **“DIRTY WAVEFORMS (DWFs)”**  
**(Zwick et al. 2022, MNRAS, 511, 6143)**



Generates high frequency harmonics *on top of the main GW*

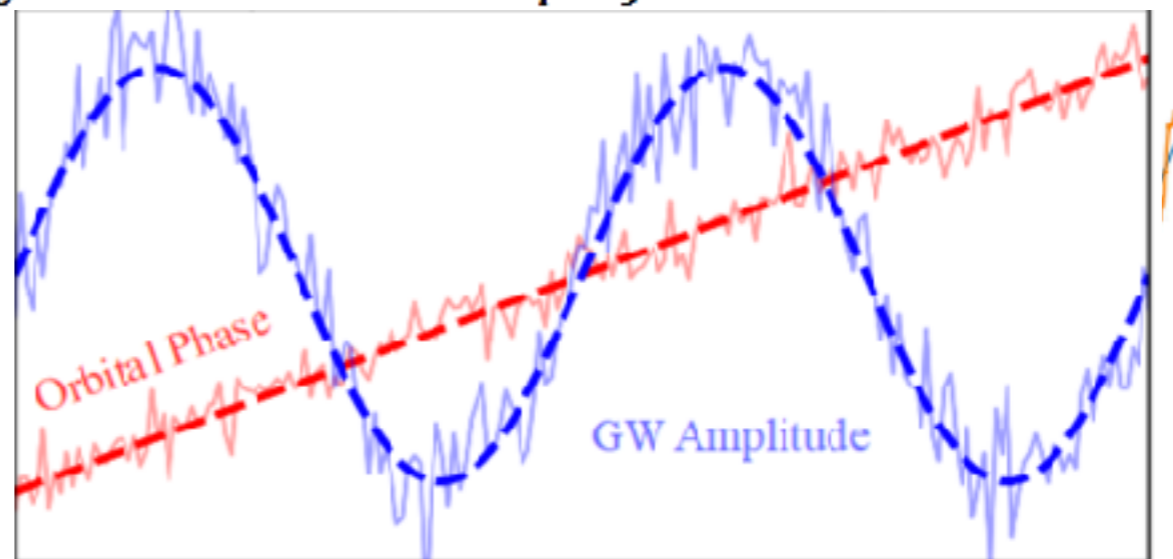
Strain of  $n^{\text{th}}$  DWF harmonic

$$|h_n^{\text{DW}}| \sim \sigma_n \frac{4G\dot{L}_{\text{lin}}}{c^4 D_L}$$

Fluctuation spectrum

$$\sigma_n = \sigma \left( \frac{l}{n} \right)^j$$

Calibrated with hydro sims + turbulence model



Typically:  $10^{-5}$  to  $10^{-3}$  of carrier  
 Typically:  $10^2/q$  harmonics

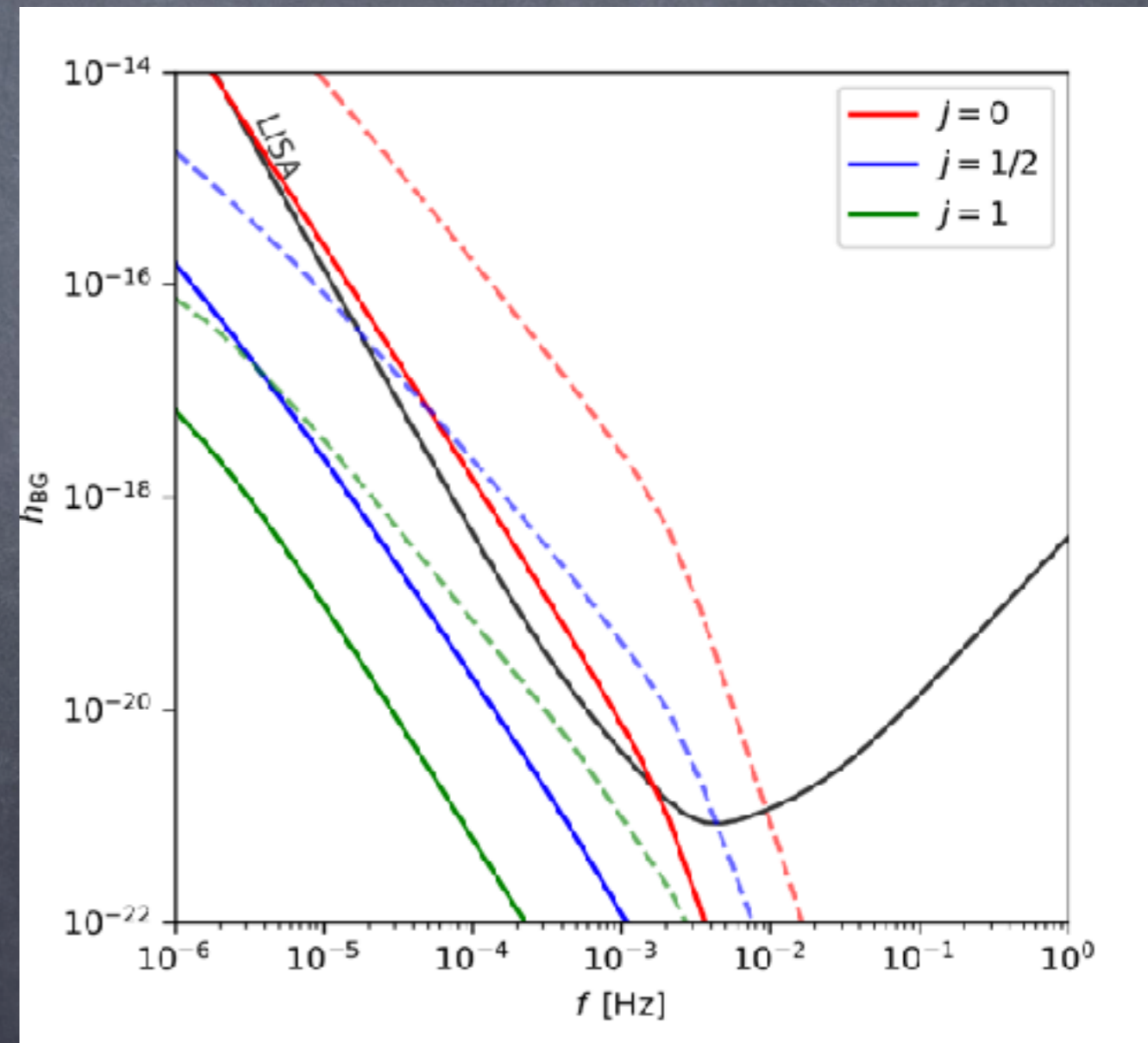
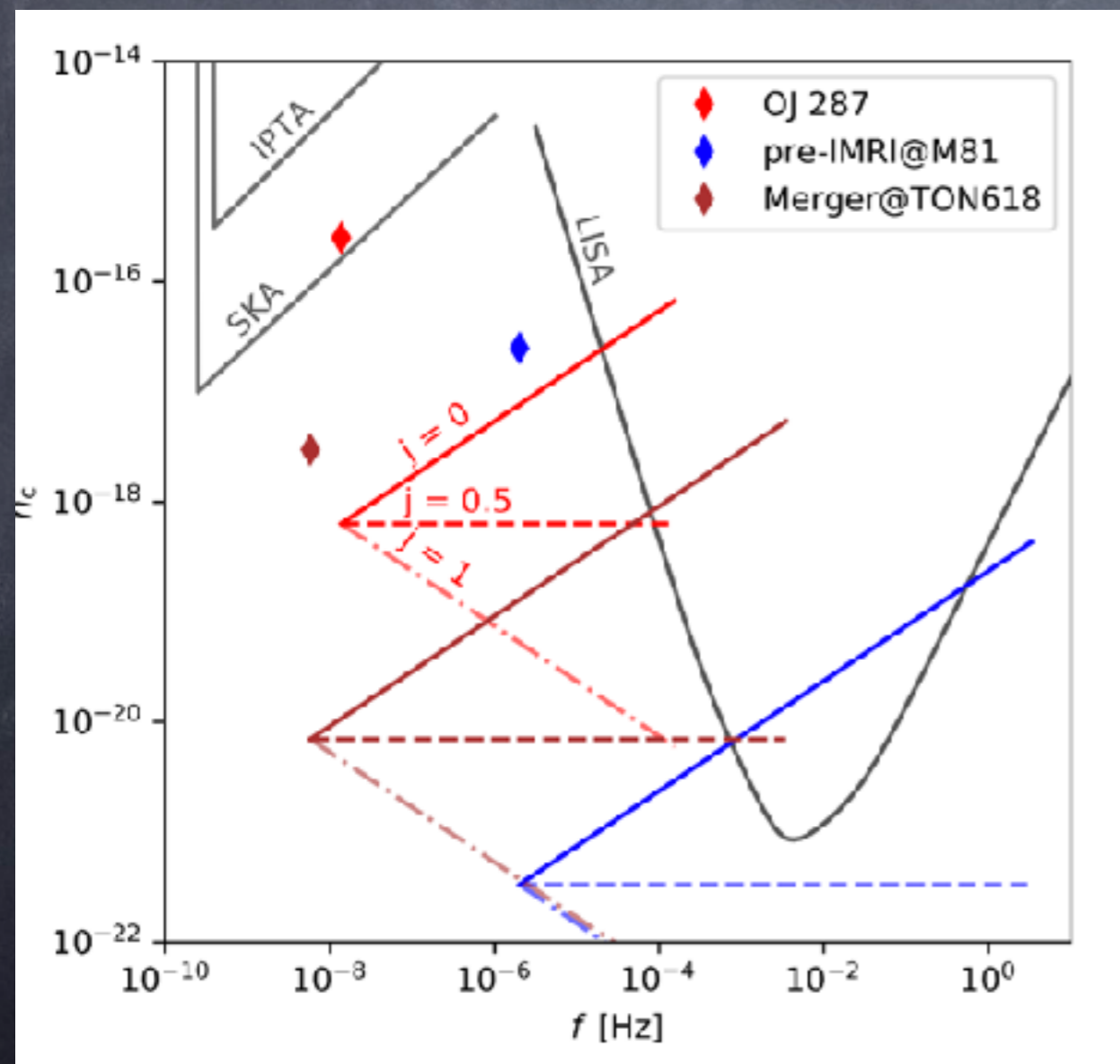
$l$  = number of orbits  
 $n$  = harmonic number  
 $q$  = mass ratio

# OBSERVATIONAL CONSEQUENCES IN LISA WINDOW

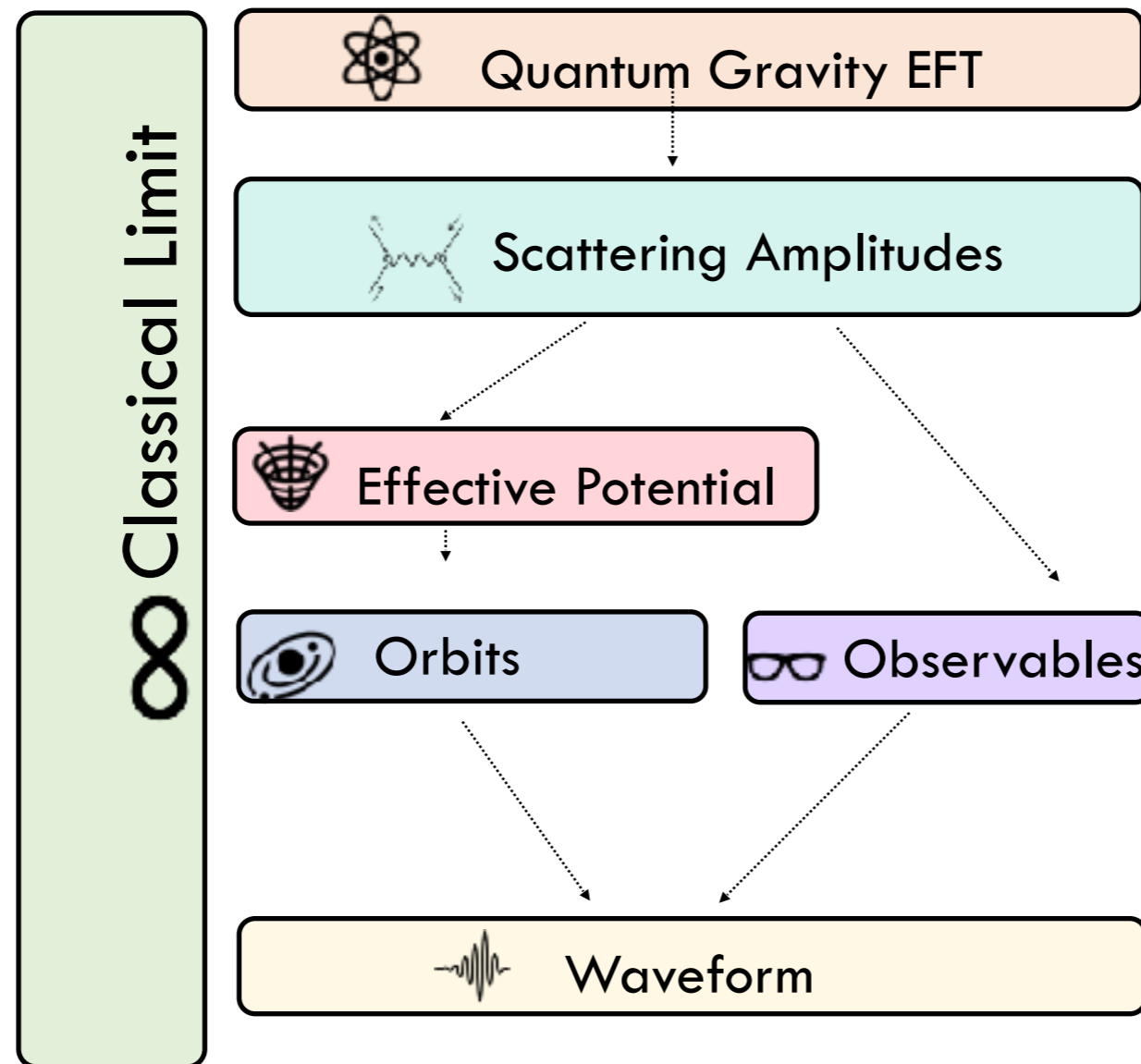
(I) low-frequency Pulsar Timing Array sources produce high-frequency DWs signal in LISA band (higher SNR compared to LISA source because SMBHs much bigger)

(III) The combination of dirty waveforms from many PTA sources produces new GW background in LISA  $\rightarrow$  **PROPERTIES DEPEND ON ASTROPHYSICAL FLOWS GENERATING FLUCTUATIONS**

$\rightarrow$  **NEW PROBE OF ACCRETION DISK PHYSICS!**



# Waveforms from scattering Amplitude Methods in the PM limit



**PhD students  
Lara Bohnenblust  
and Noemi Fabri  
Co-supervised  
by Mayer and Ita**

**Collaboration with groups of Prof. Zvi Bern (UCLA) and Prof. David Kosower (CEA, Saclay), the pioneers of scattering amplitudes applications to gravity**

# PN vs. PM

Post-Newtonian (PN) is the slow motion and weak field approximation:

$$v/c \ll 1 \quad r_S/r \sim G \ll 1$$

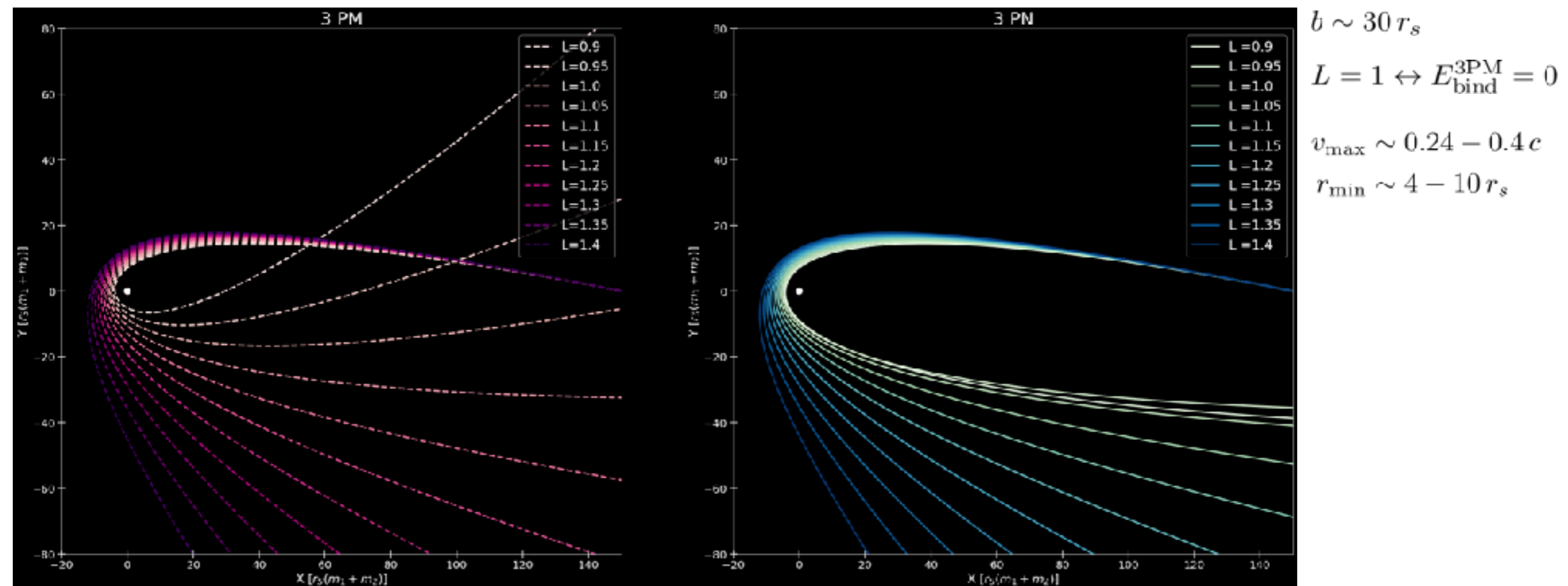
Post-Minkowskian (PM) is only the weak field approximation:  $r_S/r \sim G \ll 1$

	0PN	1PN	2PN	3PN	4PN	5PN	6PN	7PN	
1PM	( 1 )	+ v <sup>2</sup>	+ v <sup>4</sup>	+ v <sup>6</sup>	+ v <sup>8</sup>	+ v <sup>10</sup>	+ v <sup>12</sup>	+ v <sup>14</sup>	+ ... ) G <sup>1</sup>
2PM		( 1	+ v <sup>2</sup>	+ v <sup>4</sup>	+ v <sup>6</sup>	+ v <sup>8</sup>	+ v <sup>10</sup>	+ v <sup>12</sup>	+ ... ) G <sup>2</sup>
3PM			( 1	+ v <sup>2</sup>	+ v <sup>4</sup>	+ v <sup>6</sup>	+ v <sup>8</sup>	+ v <sup>10</sup>	+ ... ) G <sup>3</sup>
4PM				( 1	+ v <sup>2</sup>	+ v <sup>4</sup>	+ v <sup>6</sup>	+ v <sup>8</sup>	+ ... ) G <sup>4</sup>
5PM					( 1	+ v <sup>2</sup>	+ v <sup>4</sup>	+ v <sup>6</sup>	+ ... ) G <sup>5</sup>
6PM						( 1	+ v <sup>2</sup>	+ v <sup>4</sup>	+ ... ) G <sup>6</sup>
							⋮		

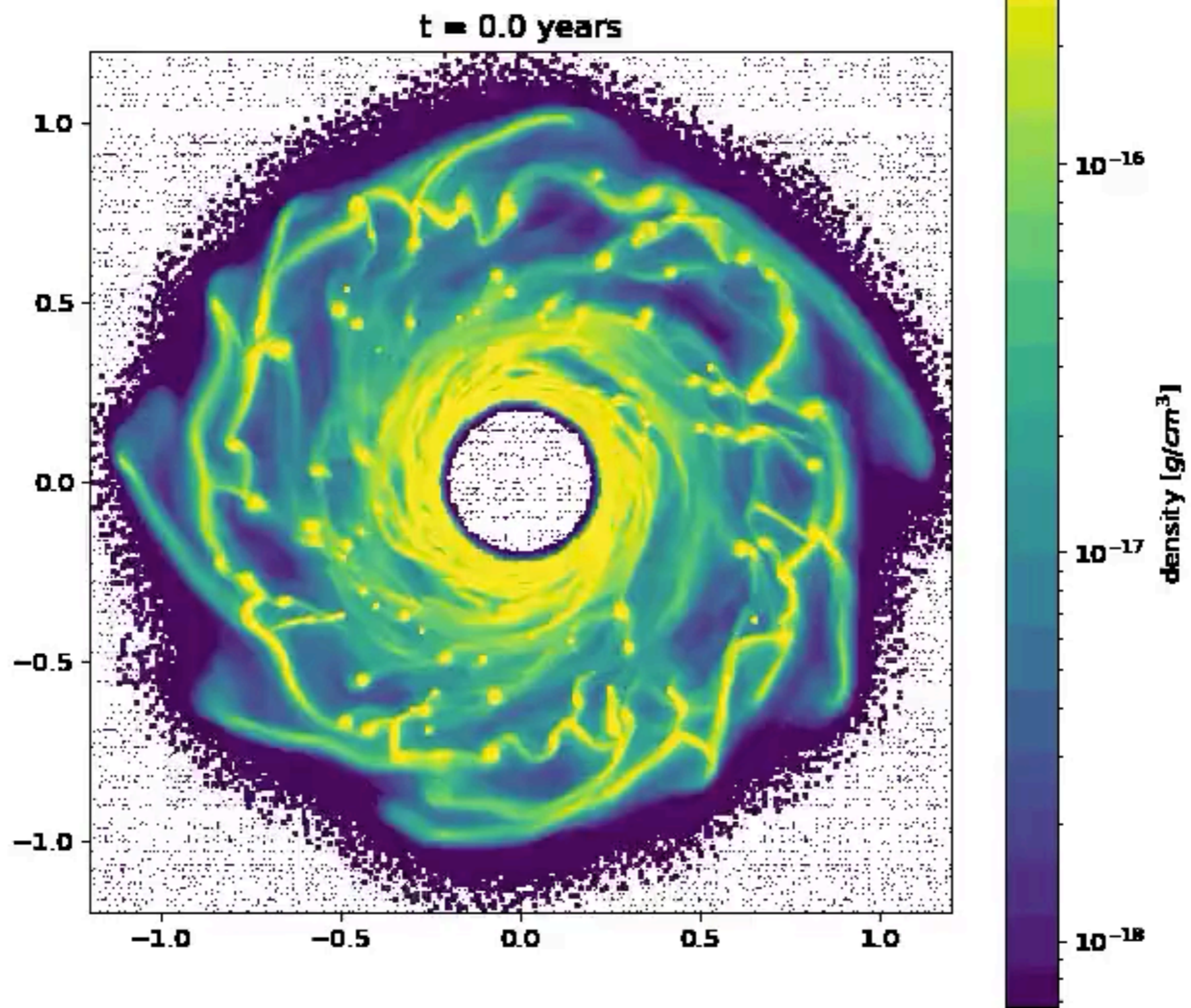
Bern et al., 2019

# Black Hole Pairs on Hyperbolic Orbits

Results from Orbit Integration PM vs. PN (Bohnenblust et al. in preparation)  
Method of Integration: *Implicit midpoint method* with adaptive timestep



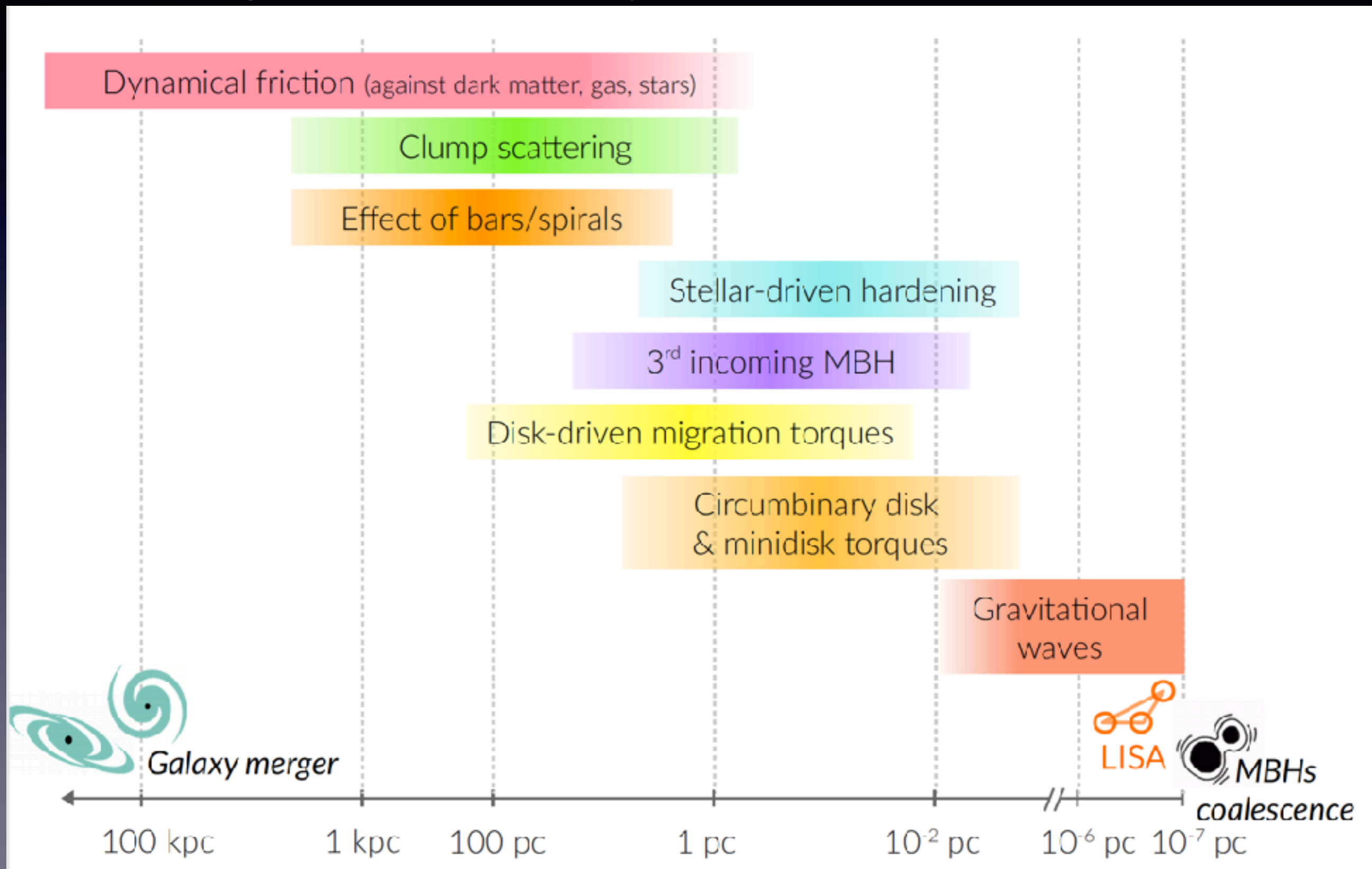
**Note: only existing published work so far used PN approximation (Cho et al. 2018)**



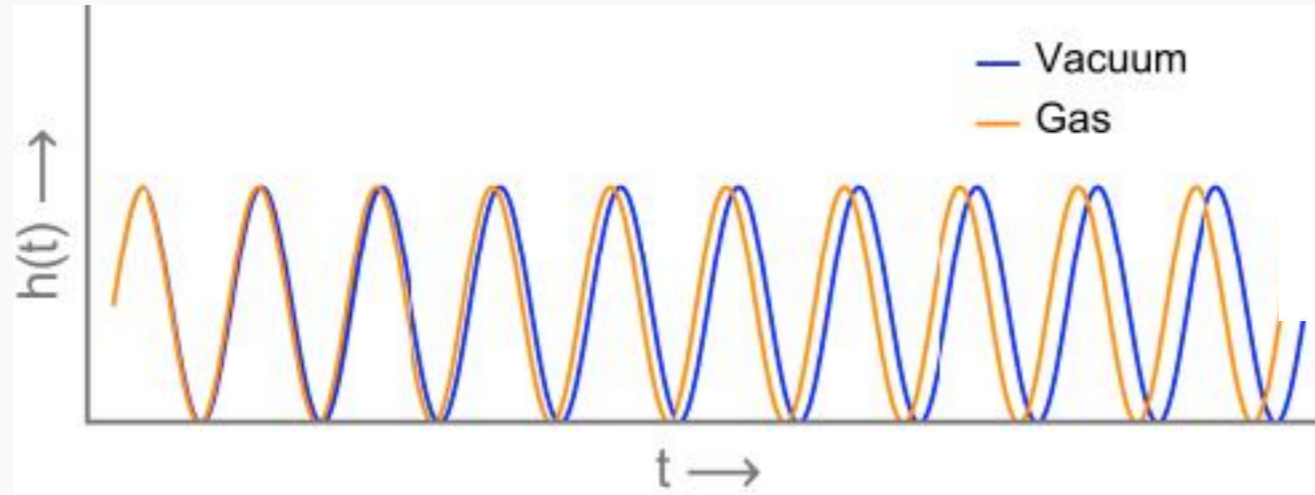
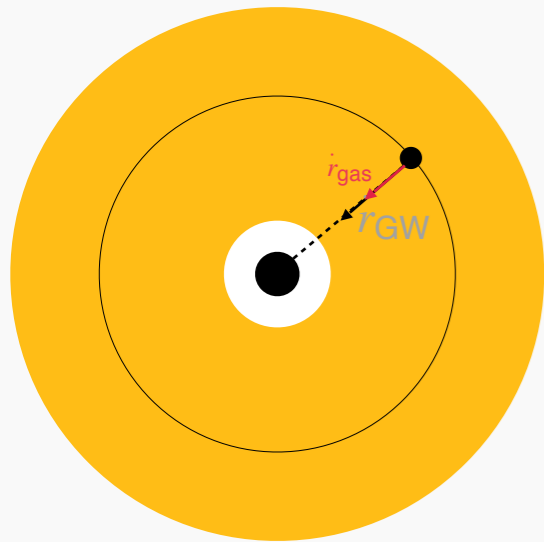


# (a) Code comparison on MBH binary decay in circumnuclear and circumbinary disks: background motivation

The path to MBH binary formation and coalescence



# Effect #1: De-phasing in the GW waveform induced by gas torques (Garg et al, to be submitted)



$$\Phi = 2\pi \int_{r_{\min}}^{r_{\max}} dr \frac{f_r}{\dot{r}}$$

$$\delta\phi = |\Phi(\dot{r}_{\text{GW}}) - \Phi(\dot{r}_{\text{GW}} + \dot{r}_{\text{gas}})| \approx$$

$$\dot{r}_{\text{gas}} \ll \dot{r}_{\text{GW}}$$

BHs decay faster (i.e BHs perform more orbits) than with just GW emission alone  $\rightarrow$  corresponds to phase change

## Assumptions & Relations

- Stationary phase approximation: **gas affect phase not amplitude**
- between LISA entry and exit/ISCO
- change in the number of orbits

## See also:

Kocsis et al. (2011), Yunes et al. (2011),  
Barausse et al. (2014), Derdzinski et al. (2019, 2021)